

$$1) \int_3^{\infty} \frac{1}{(x-2)^{3/2}} dx$$

$$2) \int_{-\infty}^0 2^r dr$$

$$3) \int_0^{\infty} \frac{x^2}{\sqrt{1+x^3}} dx$$

$$4) \int_{-\infty}^{\infty} x e^{-x^2} dx$$

$$5) \int_{-\infty}^{\infty} \cos \pi t dt$$

$$6) \int_1^{\infty} \frac{1}{x^2+x} dx$$

$$7) \int_1^{\infty} \frac{\ln x}{x^3} dx$$

$$8) \int_2^3 \frac{1}{\sqrt{3-x}} dx$$

$$9) \int_{-2}^{14} \frac{dx}{\sqrt[4]{x+2}}$$

$$10) \int_0^9 \frac{1}{\sqrt[3]{x-1}} dx$$

$$11) \int_0^8 \frac{1}{(x-6)^3} dx$$

12) Sketch the region enclosed by given curves and find its area:

~~12a.~~ a. $y = 12 - x^2$, $y = x^2 - 6$

~~12b.~~ b. $y = e^x$, $y = x e^x$, $x = 0$

c. $x = 2y^2$, $x = 4 + y^2$

e. $y = 1/x$, $y = x$, $y = \frac{1}{4}x$, $x > 0$

d. $x = y^4$, $y = \sqrt{2-x}$, $y = 0$

13) Find the number b such that line $y = b$ divides the region bounded by the curves $y = x^2$ and $y = 4$ into two regions with equal areas.

14) Find the volume of the solid obtained by rotating the region bounded by given curves about specified lines. ~~Sketch~~ Sketch the region, the solid, and a typical disk or washer.

a. $y = 2^{-1/2}x$, $y = 0$, $x = 1$, $x = 2$; about the x -axis

b. $y = 1 - x^2$, $y = 0$; about the x -axis.

c. $x = 2\sqrt{y}$, $x = 0$, $y = 9$; about the y -axis.

d. $y = x^3$, $y = x$, $x > 0$; about the x -axis

e. $y^2 = x$, $x = 2y$; about the y -axis

f. $y = 1/4 x^2$, $x = 2$, $y = 0$; about the y -axis

g. $y = x$, $y = \sqrt{x}$; about $y = 1$

h. $y = x$, $y = \sqrt{x}$; about $x = 2$

15) Find the volume of the described solid S . A right circular cone with height h and base radius r .

16) Use the method of cylindrical shells to find the volume generated by rotating the region bounded by given curves about the y -axis

a. $y = \sqrt{x}$, $y = 0$, $x = 1$

b. $y = 4x - x^2$, $y = x$

c. $y = x^2$, $y = 6x - 2x^2$

17) Let V be the volume of the solid obtained by rotating about the y -axis the region bounded by $y = \sqrt{x}$ and $y = x^2$. Find V both by slicing and by cylindrical shells. In both cases, draw a diagram to explain your method.

18) Use the method of cylindrical shells to find the volume of the solid obtained by rotating the region bounded by ~~the~~ the given curves about the x -axis.

a. $x = y = 1, x = 0, y = 1, y = 3$ b. $x = 4y^2 - y^3, x = 0$

19) Use the method of cylindrical shells to find the volume generated by rotating the region bounded by the given curves about ~~the~~ the specified axis.

a. $y = x^4, y = 0, x = 1$; about $x = 2$

b. $y = \sqrt{x}, y = 0, x = 1$; about $x = -1$

c. $y = x^3, y = 0, x = 1$; about $y = 1$

20) Use cylindrical shells to find the volume of the solid.

a. A sphere of radius r

b. A right circular cone with height h and base radius r

21) Use the arc length formula to find the length of the curve $y = 2x - 5, -1 \leq x \leq 3$. Check your answer by noting that the curve is a line segment and calculating its length by the distance formula.

22) Use the arc length formula to find the length of the curve $y = \sqrt{2-x^2}, 0 \leq x \leq 1$. Check your answer by noting that the curve is a part of a circle.

23) Find the exact length of the curve:

a. $y = 1 + 6x^{3/2}$, $0 \leq x \leq 1$

b. $y^2 = 4(x+1)^3$, $0 \leq x \leq 2$, $y > 0$

c. $y = \frac{x^3}{3} + \frac{1}{4x}$, $1 \leq x \leq 2$

d. $x = \frac{y^4}{8} + \frac{1}{4y^2}$, $1 \leq y \leq 2$

e. $x = \frac{1}{3} \sqrt{y} (y-3)$, $1 \leq y \leq 9$

f. $y = \ln(\sec x)$, $0 \leq x \leq \pi/4$

j. $y = \ln(1-x^2)$, $0 \leq x \leq \frac{1}{2}$