

$Y = \text{viscosity}$

$A = \text{Concentration} \quad - \quad +$

$B = \text{feedrate} \quad - \quad +$

$2^2 = 4$

Yates - full factorial

2^{n-1} low, 2^{n-1} high

	<u>A</u>	<u>B</u>	<u>Y</u>
1	-	-	145
2	+	-	154
3	-	+	132
4	+	+	149
<hr/>			
5	-	-	147
6	+	-	150
7	-	+	137
8	+	+	152

Special notation

	<u>A</u>	<u>B</u>	<u>AB</u>			<u>Total</u>
(1)	-	-	+	145	147	292
a	+	-	-	154	150	304
b	-	+	-	132	137	269
ab	+	+	+	149	152	301

Grand mean = 145.75

Contrast

$$\begin{aligned} A &= a + ab - (1) - b \\ &= 304 + 301 - 292 - 269 \\ &= 44 \end{aligned}$$

$$\begin{aligned} B &= 269 + 301 - 292 - 304 \\ &= -26 \end{aligned}$$

$$\begin{aligned} AB &= (1) + ab - a - b \\ &= 292 + 301 - 304 - 269 \\ &= 20 \end{aligned}$$

$$\text{Effect} = \frac{\text{Contrast}}{n 2^{k-1}}$$

$k=2$
 $n=2$
 $k = \#$ of factors
 $n = \#$ of reps

$$\text{Effect } A = \frac{44}{(2) 2^{2-1}} = \frac{44}{4} = 11$$

$$\text{Effect } B = \frac{-26}{4} = -6.5$$

$$\text{Effect } AB = \frac{20}{4} = 5$$

<u>Term</u>	<u>Effect</u>	<u>Coefficient</u>
Constant	145.75	145.75
A	11	5.5
B	-6.5	-3.25
AB	5	2.5

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x_1 + \hat{\beta}_2 x_2 + \hat{\beta}_3 x_1 x_2$$

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1(A) + \hat{\beta}_2(B) + \hat{\beta}_3(A)(B)$$

$$\hat{y} = 145.75 + 5.5(A) - 3.25(B) + 2.5(A)(B)$$

Predict viscosity will be at low level
 concent. (A) and high level
 (B) feed rate (A) -1
 (B) +1

$$\hat{y} = 145.75 + 5.5(-1) - 3.25(1) + 2.5(-1)(1)$$

$$SS = \frac{(\text{contrast})^2}{n2^k}$$

$$SS_A = \frac{(44)^2}{2(2^2)} = 242$$

$$SS_B = \frac{(-26)^2}{2(2^2)} = 84.5$$

$$SS_{AB} = \frac{(20)^2}{2(2^2)} = 50$$

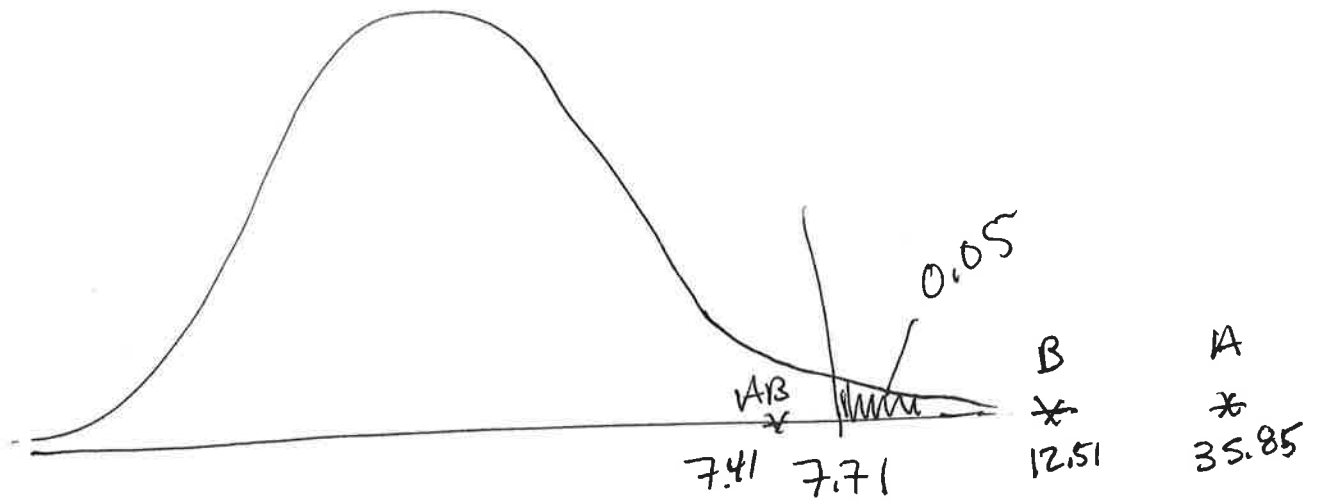
ANOVA

<u>Source of Variation</u>	<u>SS</u>	<u>DF</u>	<u>Mean Square</u>	<u>F</u>
A	242	1	242	35.85
B	84.5	1	84.5	12.51
AB	50	1	50	7.41
Error	27	4	6.75	
Total	403.5	7		

$$SS_T = \left[\begin{array}{l} 145^2 + 154^2 + 132^2 + 149^2 + \\ 147^2 + 150^2 + 137^2 + 152^2 \end{array} \right] - \frac{[292 + 304 + 269 + 301]^2}{8}$$

~~23104~~

~~403.5~~



$$H_0: \hat{\beta}_A = 0 \quad \text{Reject}$$

$$H_0: \hat{\beta}_B = 0 \quad \text{Reject}$$

$$H_0: \hat{\beta}_{AB} = 0 \quad \text{Do not reject.}$$

Factor A & B are significant

Interaction AB is not