

Assignment

Substructure Design (CE7113)

Name: Manohar Mitta

KU Id: K2004168

Date: 01-02-2021.

1) Design of pad footing

i) Design of A_1 pad footing:

The assigned parameters for footing A_1 .

Vertical Load (D.L) $V_{GK} = 455 \text{ kN}$

Vertical Live Load (L.L) $V_{QK} = 273 \text{ kN}$

V_{GK} eccentricity = 0 from both ways •

V_{QK} eccentricity = 0 from both ways •

Moment due to D.L (M_{GK}) for axis A-A = 87 kN.m

Moment due to D.L (M_{GK}) for axis 1-1 = 109 kN.m

Moment due to L.L (M_{QK}) for axis A-A = 84 kN.m

Moment due to L.L (M_{QK}) for axis 1-1 = 113 kN.m

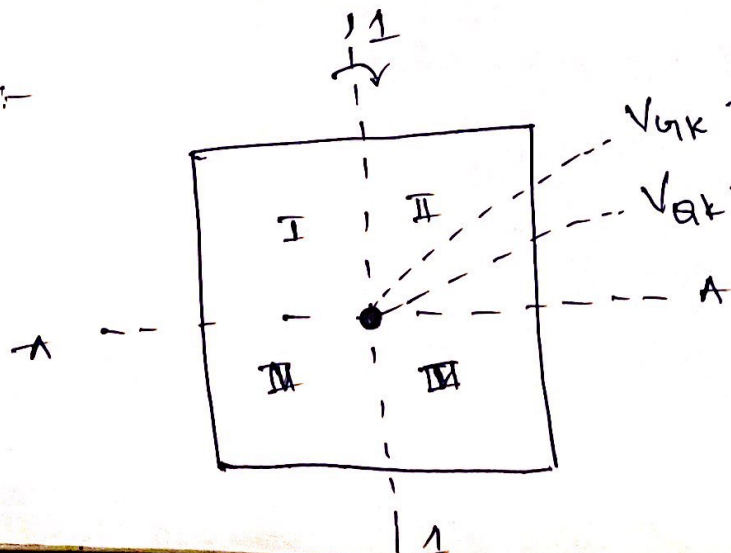
Unit weight of concrete = 25 kN/m³

Unit weight of soil = 18 kN/m³

Thickness of footing = 0.3 m

Depth

Column A_1 :-



$V_{GK} = 0$ (eccentricity)

$V_{QK} = 0$ (eccentricity)

Let assume pad length & width to be 2.3 m (2)

$$\Rightarrow \text{Self weight } (W_{GK}) = 2.3 \times 2.3 \times 0.3 \times 25 \\ = 39.68 \text{ kN}$$

$$\Rightarrow \text{Dead load } (B_{GK}) = (3 - 0.3) \times 2.3 \times 2.3 \times 18 \\ = 257.09 \text{ kN}$$

* partial factors for design loads:-

Combination 1

$$\gamma_{G1} = 1.35$$

$$\gamma_{Q1} = 1.5$$

$$\gamma_{Q1, fav} = 0$$

Combination 2

$$\gamma_{G2} = 1.0$$

$$\gamma_{Q2} = 1.3$$

$$\gamma_{Q2, fav} = 0$$

$$\therefore \text{Total } V_{GK} = W_{GK} + B_{GK} + V_{GK}(\text{given}) \\ = 39.68 + 257.09 + 455 \\ = 751.77 \text{ kN}$$

Now,

$$V_d = \begin{bmatrix} \text{combination 1} \\ \text{combination 2} \end{bmatrix} = \begin{bmatrix} \gamma_{G1} \times (\text{Total } V_{GK}) + [\gamma_{Q1} \times V_{GK}] - \gamma_{Q1, fav} \times V_{GK} \\ \gamma_{G2} \times (\text{Total } V_{GK}) + [\gamma_{Q2} \times V_{GK}] - \gamma_{Q2, fav} \times V_{GK} \end{bmatrix} \\ = \begin{bmatrix} 1.35 \times (751.77) + 1.5 \times 273 - 0 \\ 1 \times (751.77) + 1.3 \times 273 - 0 \end{bmatrix} \\ = \begin{bmatrix} 1424.39 \\ 1106.67 \end{bmatrix} \text{ kN}$$

Design moments based on load combination 1 & 2
 Calculations of moments on ~~axis~~ I, II, III, IV with respect to
 A-A

About axis A-A	Combination 1	Combination 2
1) $M_1 = -\gamma_{star} \times M_{Gk} - \gamma_{star} \times M_{Qk}$	$M_1 = -1.0 \times 87 - 0 \times 84$ $M_1 = -87 \text{ kN}\cdot\text{m}$	$M_1 = -1.0 \times 87 - 0 \times 84$ $= -87 \text{ kNm}$
2) $M_2 = M_1$	$M_2 = M_1 = -87 \text{ kN}\cdot\text{m}$	$M_2 = M_1 = -87 \text{ kN}\cdot\text{m}$
3) $M_3 = \gamma_{Gk} \times M_{Gk} + \gamma_{Qk} \times M_{Qk}$	$M_3 = 1.35 \times 87 + 1.5 \times 84$ $= 243.45 \text{ kNm}$	$M_3 = 1 \times 87 + 1.3 \times 84$ $= 196.2 \text{ kNm}$
4) $M_4 = M_3$	$M_4 = M_3 = 243.45 \text{ kNm}$	$M_4 = M_3 = 196.2 \text{ kNm}$

Calculations of moments on quadrant I, II, III, IV with
 axis.

About axis I-I	Combination 1	Combination 2
1) $M_1 = \gamma_{Gk} \times M_{Gk} - \gamma_{Qk} \times M_{Qk}$	$M_1 = 1.0 \times 109 - 0 \times 113$ $= 109 \text{ kNm}$	$M_1 = 1.0 \times 109 - 0 \times 113$ $= 109 \text{ kNm}$
2) $M_2 = \gamma_{Gk} \times M_{Gk} + \gamma_{Qk} \times M_{Qk}$	$M_2 = 1.35 \times 109 + 1.5 \times 113$ $= 316.65 \text{ kNm}$	$M_2 = 1.0 \times 109 + 1.3 \times 113$ $= 255.9 \text{ kNm}$
3) $M_3 = M_2$	$M_3 = M_2 = 316.65 \text{ kNm}$	$M_3 = M_2 = 255.9 \text{ kNm}$
4) $M_4 = M_1$	$M_4 = M_1 = 109 \text{ kNm}$	$M_4 = M_1 = 109 \text{ kNm}$

Maximum moments about A-A axis

$$M_d(A-A) = \begin{bmatrix} 243.45 \\ 196.2 \end{bmatrix} \text{ KNM}$$

Maximum moments about 1-1 axis

$$M_d(1-1) = \begin{bmatrix} 316.65 \\ 255.9 \end{bmatrix} \text{ KNM}$$

Effective pad footing area based on load combinations 1 & 2

$$e_{(A-A)} = \begin{bmatrix} \frac{M_d(A-A)}{V_d} \\ \frac{M_d(1-1)}{V_d} \end{bmatrix}$$

$$= \begin{bmatrix} 243.45/1424.39 \\ 196.2/1106.67 \end{bmatrix}$$

$$= \begin{bmatrix} 0.17 \\ 0.18 \end{bmatrix} \text{ m}$$

$$\therefore e_{(A-A)} < \frac{B}{6} \quad \text{Hence ok} \left[\because \frac{B}{6} = \frac{2.3}{6} = 0.38 \right]$$

Similarly,

$$e_{(1-1)} = \begin{bmatrix} \frac{M_d(1-1)}{V_d} \end{bmatrix}$$

$$= \begin{bmatrix} 316.65/1424.39 \\ 255.9/1106.67 \end{bmatrix}$$

$$= \begin{bmatrix} 0.22 \\ 0.23 \end{bmatrix} \text{ m} \quad \left[\because e_{(1-1)} < \frac{B}{6} \right] \text{ Hence ok.}$$

About A-A

About 1-1 (5)

* Effective length and width = (length and width in the direction of eccentricity) - 2 x eccentricity

* Smaller effective dimension
 $A' = L' \times B'$

* $Q_{design} (Q_{Ed})$
 $Q_{Ed} = \frac{V_d}{A'}$

$$\begin{bmatrix} (2.3 - 0.17) - 2 \times 0.17 \\ (2.3 - 0.16) - 2 \times 0.16 \end{bmatrix}$$

$$= \begin{bmatrix} 1.79 \\ 1.76 \end{bmatrix} = \begin{bmatrix} L'_1 & B'_1 \\ L'_2 & B'_2 \end{bmatrix} m$$

$$\begin{bmatrix} 3.25 \\ 3.09 \end{bmatrix} m^2$$

$$\begin{bmatrix} \frac{1424.39}{3.2} \\ \frac{1106.67}{3.09} \end{bmatrix}$$

$$= \begin{bmatrix} 445.12 \\ 358.15 \end{bmatrix}$$

$$\begin{bmatrix} (2.3 - 0.22) - 2 \times 0.22 \\ (2.3 - 0.23) - 2 \times 0.23 \end{bmatrix}$$

$$\begin{bmatrix} 0.64 \\ 0.61 \end{bmatrix} = \begin{bmatrix} L'_1 & B'_1 \\ L'_2 & B'_2 \end{bmatrix}$$

$$\begin{bmatrix} 2.68 \\ 2.59 \end{bmatrix} m^2$$

$$\begin{bmatrix} \frac{1424.39}{2.68} \\ \frac{1106.67}{2.59} \end{bmatrix}$$

$$\begin{bmatrix} 531.48 \\ 427.29 \end{bmatrix}$$

Bearing capacity (undrained condition)

$$Q_{ult} = (\pi + 2) c_u b_c s_c i_c + q$$

$$c_u = \text{SPT value} \times 5$$

$$= 20 \times 5 = 100$$

	About A-A axis	About (1-1) axis
1) undrained strength 2) c_u	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$
3) $\frac{c_u}{\gamma c_u}$	$\begin{bmatrix} \frac{100}{1} \\ \frac{100}{1.4} \end{bmatrix} = \begin{bmatrix} 100 \\ 71.42 \end{bmatrix}$	$\begin{bmatrix} \frac{100}{1} \\ \frac{100}{1.4} \end{bmatrix} = \begin{bmatrix} 100 \\ 71.42 \end{bmatrix}$
4) $b_c = \frac{1-2\alpha}{\pi+2}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
5) $s_c = 1.2$ for square or circular footing	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$
6) $i_c = 0.5 \left(1 + \frac{\sqrt{1-H}}{A' c_u} \right)$ Provided $H \leq A' c_u$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
7) $q = \text{density of soil} \times \text{depth of footing}$	$\begin{bmatrix} 18 \times 3.0 = 54 \\ 18 \times 3.0 = 54 \end{bmatrix}$ kNm	$\begin{bmatrix} 54 \\ 54 \end{bmatrix}$ kNm
8) $Q_{ult} = (\pi + 2) c_u b_c s_c i_c + q$	$\begin{bmatrix} (\pi+2) \times 100 \times 1 \times 1.2 \times 1 + 54 \\ (\pi+2) \times 71.42 \times 1 \times 1.2 \times 1 + 54 \end{bmatrix} = \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa
9) $Q_{ult} / \gamma R$	$\begin{bmatrix} 670.8 / 1 \\ 494.58 / 1 \end{bmatrix} = \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$
10) utilization factor a. $\frac{Q_{ed} \times 100}{Q_{ult}}$	$\begin{bmatrix} \frac{445.12}{670.8} \times 100 \\ \frac{358.15}{494.58} \times 100 \end{bmatrix} = \begin{bmatrix} 66.36\% \\ 72.41\% \end{bmatrix} < 100\%$	$\begin{bmatrix} \frac{531.48}{670.8} \times 100 \\ \frac{427.29}{494.58} \times 100 \end{bmatrix} = \begin{bmatrix} 79.23\% \\ 86.37\% \end{bmatrix} < 100\%$

	About axis (A-A)	About axis (1-1) \oplus
$M = \frac{L}{B'}$	$\begin{bmatrix} \frac{1.79}{1.79} \\ \frac{1.76}{1.76} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} \frac{1.64}{1.64} \\ \frac{1.61}{1.61} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$
$N = \frac{H}{B'} \quad (\because H = 4 \times B)$	$\begin{bmatrix} \frac{2.3 \times 4}{1.79} \\ \frac{2.3 \times 4}{1.76} \end{bmatrix} = \begin{bmatrix} 5.14 \\ 5.23 \end{bmatrix}$	$\begin{bmatrix} \frac{2.3 \times 4}{1.64} \\ \frac{2.3 \times 4}{1.61} \end{bmatrix} = \begin{bmatrix} 5.61 \\ 5.71 \end{bmatrix}$

$$E_s = 1000 \times Q_{uni}/2$$

$$Q_{uni} = 2 \times C_u \left[C_u = 5 \times \text{SPT value} \right]$$

$$= 2 \times 5 \times \text{SPT value}$$

$$E_s = 1000 \times 5 \times \text{SPT value}$$

$$E_s \text{ at } 3.5 = 1000 \times 5 \times 20 = 1,00,000 \text{ KPa}$$

$$E_s \text{ at } 5.5 = 1000 \times 5 \times 54 = 2,70,000 \text{ KPa}$$

$$E_s \text{ at } 8.0 = 1000 \times 5 \times 50 = 2,50,000 \text{ KPa}$$

$$E_s \text{ weighted average} = \frac{1,00,000 \times 3.5 + 2,70,000 \times 5.5 + 2,50,000 \times 8}{17}$$

$$= 2,25,588 \text{ KPa}$$

$$A_H = \gamma_0 B' \times \frac{1-M^2}{E_s} \left(I_1 + \frac{1-2M}{1-M} I_2 \right) I_F$$

$$I_1 = \frac{1}{\pi} \left[M \times \ln \frac{(1 + \sqrt{M^2+1}) \sqrt{M^2+N^2}}{M(1 + \sqrt{M^2+N^2+1})} + \ln \frac{(M + \sqrt{M^2+1}) \sqrt{1+N^2}}{M + \sqrt{M^2+N^2+1}} \right]$$

$$I_2 = \frac{N}{2\pi} \tan^{-1} \left(\frac{M}{N \sqrt{M^2+N^2+1}} \right)$$

About A-A axis

Combination 1:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (5.14)^2}}{1(1 + \sqrt{1^2 + (5.14)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (5.14)^2}}{1 + \sqrt{1^2 + (5.14)^2} + 1} \right]$$

$$= 0.44$$

$$I_2 = \frac{5.14}{2\pi} \tan^{-1} \left(\frac{1}{5.14 \sqrt{1^2 + (5.14)^2 + 1}} \right) = 1.71$$

$$\Delta_H = 4.45 \times 1.79 \times \frac{(1 - (0.3)^2)}{225588} \left(0.44 + \frac{1 - 2(0.3)}{1 - 0.3} \times 1.71 \right) \times 0.623$$

$$= 0.000283687$$

To limit settlement to 50mm $q = \frac{0.05}{0.000283687} = 176205 \text{ kN/m}^2$

Combination 2:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (5.23)^2}}{1(1 + \sqrt{1^2 + (5.23)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (5.23)^2}}{1 + \sqrt{1^2 + (5.23)^2} + 1} \right]$$

$$= 0.44$$

$$I_2 = \frac{5.23}{2\pi} \tan^{-1} \left(\frac{1}{5.23 \sqrt{1^2 + (5.23)^2 + 1}} \right) = 1.68$$

$$\Delta_H = 358.15 \times 1.79 \times \frac{1 - (0.3)^2}{223588} \left(0.44 + \frac{1 - 2(0.3)}{1 - 0.3} \times 1.68 \right) \times 0.4$$
$$= 0.0002256$$

To limit settlement to 50mm

$$q = \frac{0.05}{0.0002256} = 221.63 \text{ kN/m}^2$$

About 1-1 axis

9

Combination 1:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (5.6)^2}}{1(1 + \sqrt{1^2 + (5.6)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (5.6)^2}}{1 + \sqrt{1^2 + (5.6)^2} + 1} \right]$$
$$= 0.45$$

$$I_2 = \frac{5.6}{2\pi} \tan^{-1} \left(\frac{1}{5.6 \sqrt{1^2 + (5.6)^2 + 1}} \right) = 1.58$$

$$\Delta_H = 0.000296$$

To limit settlement to 50 mm

$$q = \frac{0.05}{0.000296} = 168.91 \text{ kN/m}^2$$

Combination 2:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (5.7)^2}}{1(1 + \sqrt{1^2 + (5.7)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (5.7)^2}}{1 + \sqrt{1^2 + (5.7)^2} + 1} \right]$$
$$= 0.45$$

$$I_2 = \frac{5.7}{2\pi} \tan^{-1} \left(\frac{1}{5.7 \sqrt{1^2 + (5.7)^2 + 1}} \right) = 1.55$$

$$\Delta_H = 427.29 \times 1.61 \times \frac{1 - (0.3)^2}{2 \times 2558.8} \left(0.45 + \frac{(-2 \times 0.3)}{1 - 0.3} \times 1.55 \right) \times 0.623$$

$$= 0.000228$$

To limit settlement to 50 mm

$$q = \frac{0.05}{0.00023} = 217 \text{ kN/m}^2$$

ii) Design of A_2 pad footing:

The assigned parameters for footing A_2

$$\text{Vertical load (D.L)} (V_{GK}) = 314 \text{ KN}$$

$$\text{Vertical live load } (V_{QK}) = 73 \text{ KN}$$

$$V_{GK} \text{ eccentricity} = 0 \text{ from both ways}$$

$$V_{QK} \text{ eccentricity} = 0 \text{ from both ways}$$

$$\text{Moment due to D.L } (M_{GK}) \text{ for axis A-A} = 98 \text{ KNM}$$

$$\text{Moment due to D.L } (M_{GK}) \text{ for axis 2-2} = 101 \text{ KNM}$$

$$\text{Moment due to L.L } (M_{QK}) \text{ for axis A-A} = 23 \text{ KNM}$$

$$\text{Moment due to L.L } (M_{QK}) \text{ for axis 2-2} = 32 \text{ KNM}$$

$$\text{Unit weight of concrete} = 25 \text{ KN/m}^3$$

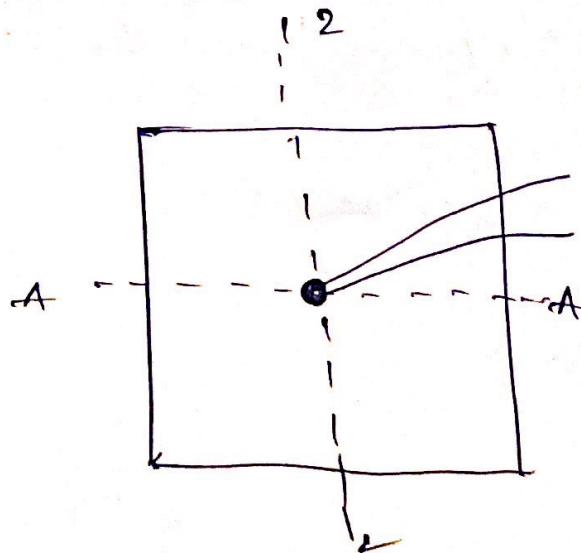
$$\text{Unit weight of soil} = 18 \text{ KN/m}^3$$

$$\text{Thickness of footing} = 0.3 \text{ m}$$

Depth

$$= 3 \text{ m}$$

Column A_2 :



V_{GK} eccentricity = 0
 V_{QK} eccentricity = 0

let assume pad length & width to be 2.3 m

$$\Rightarrow \text{self weight } (W_{GK}) = 2.3 \times 2.3 \times 0.3 \times 25 \\ = 39.68 \text{ kN}$$

$$\rightarrow \text{Dead load } (B_{GK}) = (3 - 0.3) \times 2.3 \times 2.3 \times 18 \\ = 257.09 \text{ kN}$$

* partial factors for design loads :-

Combination 1

$$\gamma_{G1} = 1.35$$

$$\gamma_{Q1} = 1.5$$

$$\gamma_{Q1, \text{fav}} = 0$$

Combination

$$\gamma_{G2} = 1.0$$

$$\gamma_{Q2} = 1.3$$

$$\gamma_{Q2, \text{fav}} = 0$$

$$\therefore \text{Total } V_{GK} = W_{GK} + B_{GK} + V_{GK}(\text{given}) \\ = 39.68 + 257.09 + 314 \\ = 610.77 \text{ kN}$$

Now,

$$V_d = \begin{bmatrix} \text{combination 1} \\ \text{combination 2} \end{bmatrix} = \begin{bmatrix} \gamma_{G1} \times (\text{Total } V_{GK}) + [\gamma_{Q1} \times V_{GK}] - \gamma_{Q1, \text{fav}} \times V_{GK} \\ \gamma_{G2} \times (\text{Total } V_{GK}) + [\gamma_{Q2} \times V_{GK}] - \gamma_{Q2, \text{fav}} \times V_{GK} \end{bmatrix}$$

$$= \begin{bmatrix} 1.35 (610.77) + 1.5 \times 73 - 0 \\ 1 \times (610.77) + 1.3 \times 73 - 0 \end{bmatrix}$$

$$= \begin{bmatrix} 934.04 \\ 705.67 \end{bmatrix} \text{ kN}$$

Design moments based on load combination 1 & 2

* Calculations of moments on quadrant I, II, III, IV w.r.t axis

(A-A)

About axis (A-A)	Combination 1	Combination 2
1) $M_1 = -\int_{GK} \text{far} \times M_{GK} - \int_{GK} \text{far} \times M_{OK}$ 2) $M_2 = M_1$ 3) $M_3 = \int_{GK} \text{far} \times M_{GK} + \int_{OK} \text{far} \times M_{OK}$ 4) $M_u = M_3$	1) $M_1 = -1.0 \times 98 - 0 \times 23$ $M_1 = -98 \text{ kNm}$ 2) $M_2 = M_1 = -98 \text{ kNm}$ 3) $M_3 = 1.35 \times 98 + 1.5 \times 23$ $= 166.8 \text{ kNm}$ 4) $M_u = M_3 = 166.8 \text{ kNm}$	$M_1 = -1.0 \times 98 - 0 \times 23$ $M_1 = -98 \text{ kNm}$ $M_2 = M_1 = -98 \text{ kNm}$ $M_3 = 1 \times 98 + 1.3 \times 23$ $= 127.9 \text{ kNm}$ $M_u = M_3 = 127.9 \text{ kNm}$

* Calculations of moments on quadrants I, II, III and IV w.r.t 2-2

About axis (2-2)	Combination 1	Combination 2
1) $M_1 = \int_{GK} \text{far} \times M_{GK} - \int_{OK} \text{far} \times M_{OK}$ 2) $M_2 = (\int_{GK} \text{far} \times M_{GK}) + (\int_{OK} \text{far} \times M_{OK})$ 3) $M_3 = M_2$ 4) $M_u = M_1$	$M_1 = 1 \times 101 - 0 \times 32$ $= 101 \text{ kNm}$ $M_2 = 1.35 \times 101 + 1.5 \times 32$ $= 184.35 \text{ kNm}$ $M_3 = M_2 = 184.35 \text{ kNm}$ $M_u = M_1 = 101 \text{ kNm}$	$M_1 = 1 \times 101 - 0 \times 32$ $= 101 \text{ kNm}$ $M_2 = 1 \times 101 + 1.3 \times 32$ $= 142.6 \text{ kNm}$ $M_3 = M_2 = 142.6 \text{ kNm}$ $M_u = M_1 = 101 \text{ kNm}$

Maximum moments about 1-1 axis

$$M_d(1-1) = \begin{bmatrix} 166.8 \\ 127.9 \end{bmatrix} \text{ kNm}$$

Maximum moments about 2-2 axis

$$M_d(2-2) = \begin{bmatrix} 184.35 \\ 142.6 \end{bmatrix} \text{ kNm}$$

Effective pad footing area based on load combinations 1.42

$$e_{(1-1)} = \begin{bmatrix} \frac{M_d(1-1)}{V_d} \\ \frac{166.8/934.04}{127.9/705.67} \end{bmatrix} = \begin{bmatrix} 0.18 \\ 0.18 \end{bmatrix} \text{ m}$$

∴

$$\therefore e_{(1-1)} < \frac{B}{6} \text{ Hence ok } \left[\because \frac{B}{6} = \frac{2.3}{6} = 0.38 \right]$$

Similarly

$$e_{(2-2)} = \begin{bmatrix} \frac{M_d(2-2)}{V_d} \\ \frac{184.35/934.04}{142.6/705.67} \end{bmatrix} = \begin{bmatrix} 0.20 \\ 0.20 \end{bmatrix} \text{ m}$$

$$\therefore e_{(2-2)} < \frac{B}{6} \text{ Hence ok.}$$

About A-A axis

About Z-Z axis

* Effective length and width
 = (length and width in the direction of eccentricity)
 → 2 x eccentricity

$$\begin{bmatrix} (2.3 - 0.18) - 2 \times 0.18 \\ (2.3 - 0.18) - 2 \times 0.18 \end{bmatrix}$$

$$\begin{bmatrix} (2.3 - 0.2) - 2 \times 0.2 \\ (2.3 - 0.2) - 2 \times 0.2 \end{bmatrix}$$

$$= \begin{bmatrix} 1.76 \\ 1.76 \end{bmatrix} = \begin{bmatrix} L' & A B' \\ L' & A B' \end{bmatrix}$$

$$= \begin{bmatrix} 1.676 \\ 1.70 \end{bmatrix}$$

* Smaller effective dimensions

$$A' = L' \times B'$$

$$= \begin{bmatrix} 3.1 \\ 3.1 \end{bmatrix}$$

$$= \begin{bmatrix} 2.89 \\ 2.89 \end{bmatrix}$$

* σ_{design}
 $(\sigma_{Ed}) = \frac{V_d}{A'}$

$$= \begin{bmatrix} \frac{934.04}{3.1} \\ \frac{705.67}{3.1} \end{bmatrix}$$

$$\begin{bmatrix} \frac{934.04}{2.89} \\ \frac{705.67}{2.89} \end{bmatrix}$$

$$= \begin{bmatrix} 301.3 \\ 227.64 \end{bmatrix}$$

$$= \begin{bmatrix} 323.20 \\ 244.18 \end{bmatrix}$$

Bearing capacity (undrained condition)

$$Q_{ult} = (\pi + 2) C_u b_c S_c i_c + q$$

$$C_u = \text{SPT value} \times 5$$

$$= 20 \times 5 = 100$$

	About A-A axis	About (2-2) axis
1. Undrained strength (C_u)	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$
2) $\frac{C_u}{\gamma C_u}$	$\begin{bmatrix} 100/1 \\ 100/1.4 \end{bmatrix} = \begin{bmatrix} 100 \\ 71.43 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 71.42 \end{bmatrix}$
3. $b_c = \frac{1-2\alpha}{\pi+2}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
4. $S_c = 1.2$ for square or circular footing	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$
5. $i_c = 0.5 \left(1 + \sqrt{1 - \frac{H}{\pi C_u}}\right)$ provided $H \leq \pi C_u$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
6. $q =$ density of soil \times depth of footing	$\begin{bmatrix} 18 \times 3.0 = 54 \\ 18 \times 3.0 = 54 \end{bmatrix}$ kNm	$\begin{bmatrix} 54 \\ 54 \end{bmatrix}$ kNm
7 $Q_{ult} = (\pi + 2) C_u b_c S_c i_c + q$	$\begin{bmatrix} (\pi + 2) \times 100 \times (1.2 \times 1) + 54 \\ (\pi + 2) \times 71.43 \times (1.2 \times 1) + 54 \end{bmatrix}$ $= \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa
8. $Q_{ult} / \gamma R$	$\begin{bmatrix} 670.8/1 \\ 494.58/1 \end{bmatrix} = \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$
9. Utilization factor $= \frac{Q_{ed}}{Q_{ult}} \times 100$	$\begin{bmatrix} \frac{301.3}{670.8} \times 100 \\ \frac{227.64}{494.58} \times 100 \end{bmatrix} = \begin{bmatrix} 44.92\% \\ 46.03\% \end{bmatrix}$ $< 100\%$	$\begin{bmatrix} \frac{523.20}{670.8} \times 100 \\ \frac{244.15}{494.58} \times 100 \end{bmatrix} = \begin{bmatrix} 78.14\% \\ 49.37\% \end{bmatrix}$ $< 100\%$ Hence ok

	About axis (A-A)	About axis (2-2)
$M = \frac{L}{B'}$	$\begin{bmatrix} \frac{1.76}{1.76} \\ \frac{1.76}{1.76} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} \frac{1.7}{1.7} \\ \frac{1.7}{1.7} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$
$N = \frac{H}{B'} \quad [\because H = 4 \times B]$	$\begin{bmatrix} \frac{7.2}{1.76} \\ \frac{7.2}{1.76} \end{bmatrix} = \begin{bmatrix} 5.23 \\ 5.23 \end{bmatrix}$	$\begin{bmatrix} \frac{9.2}{1.7} \\ \frac{9.2}{1.7} \end{bmatrix} = \begin{bmatrix} 5.41 \\ 5.41 \end{bmatrix}$

$$E_s = 1000 \times Q_{uni} / 2$$

$$Q_{uni} = 2 \times C_u \quad [\because C_u = 5 \times \text{SPT value}]$$

$$= 2 \times 5 \times \text{SPT value}$$

$$E_s \text{ at } 3.5 \text{ m} = 1000 \times 5 \times 20 = 100,000 \text{ kpc}$$

$$E_s \text{ at } 5.5 \text{ m} = 1000 \times 5 \times 54 = 2,70,000 \text{ kpc}$$

$$E_s \text{ at } 8.0 \text{ m} = 1000 \times 5 \times 80 = 4,00,000 \text{ kpc}$$

$$E_s \text{ weighted average} = \frac{100,000 \times 3.5 + 2,70,000 \times 5.5 + 4,00,000 \times 8}{13} = 22382 \text{ kpc}$$

$$\Delta_u = q_0 B' \times \frac{1-u^2}{E_s} \left(I_1 + \frac{1-2u}{1-u} I_2 \right) I_F$$

$$I_1 = \frac{1}{\pi} \left[M \times \ln \frac{(1 + \sqrt{1+M^2} \sqrt{M^2+N^2})}{M + (1 + \sqrt{M^2+N^2})} + \ln \frac{(M + \sqrt{M^2+1} \sqrt{1+N^2})}{M + \sqrt{M^2+N^2+1}} \right]$$

$$I_2 = \frac{N}{2\pi} \tan^{-1} \left(\frac{M}{N \sqrt{M^2+N^2+1}} \right)$$

About 2-2 axis

Combination 1:

$$\frac{I_1}{I} = \frac{1}{\pi} \left[1 + \ln \frac{(1 + \sqrt{1^2 + 1} \sqrt{1^2 + (5.41)^2})}{(1 + \sqrt{1^2 + (5.41)^2} + 1)} \right] + \ln \frac{(1 + \sqrt{1^2 + 1} \sqrt{1 + (5.41)^2})}{1 + \sqrt{1^2 + (5.41)^2} + 1}$$

$$= 0.45$$

$$I_2 = \frac{5.41}{2\pi} \tan^{-1} \left(\frac{1}{5.41 \sqrt{1^2 + (5.41)^2} + 1} \right) = 1.63$$

$$\Delta_H = 323.20 \times 1.7 \times \frac{1 - 0.3^2}{22582} \left(0.45 + \frac{1 - 2(0.3)}{1 - 0.3} \times 1.63 \right) 0.623$$

$$= 0.000192$$

∴ limit settlement to 50mm $\Rightarrow \frac{0.05}{0.000192} = 260 \text{ kN/m}^2$

Combination 2

similarly,

$$I_1 = 0.45$$

$$I_2 = 1.63$$

$$\Delta_H = 244.18 \times 1.7 \times \frac{1 - 0.3^2}{22362} \left(0.45 + \frac{1 - 2(0.3)}{1 - 0.3} \times 1.63 \right) 0.623$$

$$= 200 \cdot 0.000145$$

∴ limit settlement to 50mm

$$q = \frac{0.05}{0.000145} = 344.82 \text{ kN/m}^2$$

iii) Design of B_1 pad footing

The assigned parameters for footing B_1

Vertical load (dead load) $V_{GK} = 836 \text{ kN}$

Vertical live load $V_{QK} = 198 \text{ kN}$

V_{GK} eccentricity = 0 both ways

V_{QK} eccentricity = $0.1 B$ both ways

Moment due to D.L (M_{GK}) for axis 1-1 = ~~58~~ 58 kNm

Moment due to L.L (M_{QK}) for axis 1-1 = 52 kNm

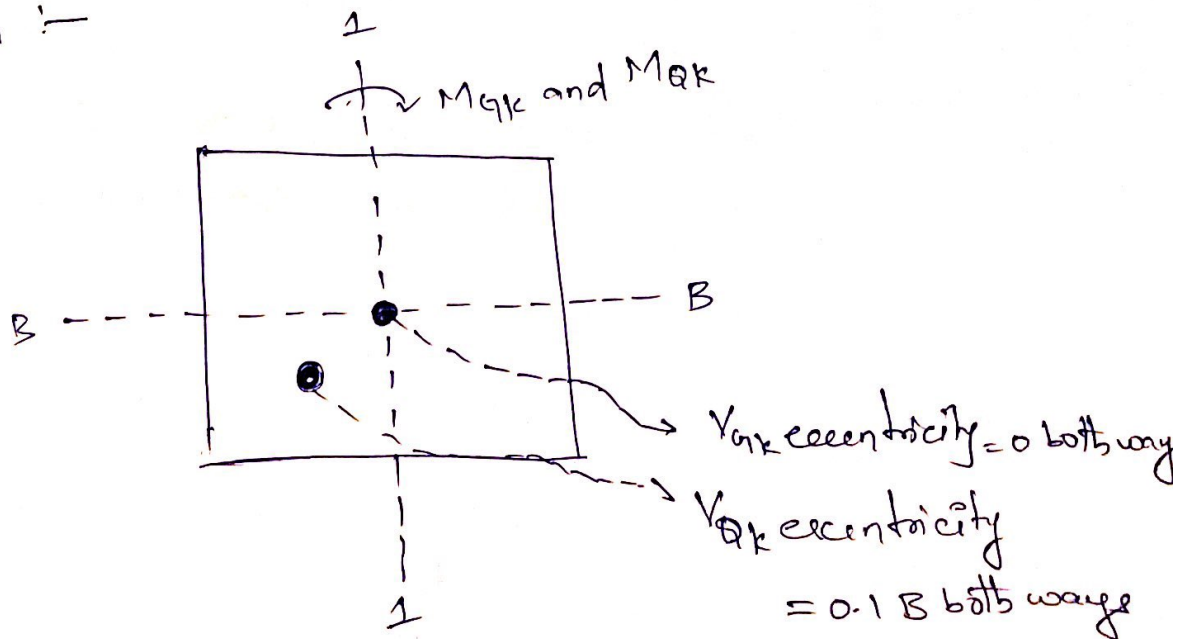
Unit weight of concrete = 25 kN/m^3

Unit weight of soil = 18 kN/m^3

Thickness of footing = 0.3 m

Depth = 3 m

Column B_1 :-



Let assume pad length & width to be 2.3m

$$\Rightarrow \text{self weight } (W_{GK}) = 2.3 \times 2.3 \times 0.3 \times 25 \\ = 39.68 \text{ kN}$$

$$\Rightarrow \text{Dead load } (B_{GK}) = (3 - 0.3) \times 2.3 \times 2.3 \times 14 \\ = 257.09 \text{ kN}$$

* partial factors for design loads:-

$$\gamma_{G1} = 1.35 \qquad \gamma_{G2} = 1.0$$

$$\gamma_{Q1} = 1.5 \qquad \gamma_{Q2} = 1.3$$

$$\gamma_{Q1, fav} = 1 \qquad \gamma_{G1, fav} = 1$$

$$\gamma_{Q1, fav} = 0 \qquad \gamma_{Q1, fav} = 0$$

$$\therefore \text{Total } V_{GK} = W_{GK} + B_{GK} + V_{GK}(\text{given})$$

$$= 39.68 + 257.09 + 836$$

$$= 1132.77 \text{ kN}$$

Now,

$$V_d = \begin{bmatrix} \text{Combination 1} \\ \text{Combination 2} \end{bmatrix} = \begin{bmatrix} \gamma_{G1} (\text{total } V_{GK}) + (\gamma_{Q1} \times V_{QK} - \gamma_{Q1, fav} \times 0_{KB}) \\ \gamma_{G2} (\text{total } V_{GK}) + (\gamma_{Q2} \times V_{QK} - \gamma_{Q1, fav} \times 0_{KB}) \end{bmatrix}$$

$$= \begin{bmatrix} 1.35 (1132.77) + 1.5 \times 198 - 0 \\ 1.0 \times 1132.77 + 1.3 (198 - 0) \end{bmatrix}$$

$$= \begin{bmatrix} 1826.24 \\ 1390.17 \end{bmatrix} \text{ kN}$$

Design moments based on Load Combination 1 & 2
 * calculations of moments on quadrant I, II, III, IV w.r.t
 axis (B-B) and axis (1-1)

About axis (B-B)	Combination 1	Combination 2
1) $M_1 = -\cancel{2.3} (0) + (0) - \sqrt{2} \times 0.1B \times V_{ok}$ 2) $M_2 = M_1$ 3. $M_3 = (0) + (0) + \sqrt{2} \times 0.1B \times V_{ok}$ 4. $M_3 = M_4$	$M_1 = -1.5 \times 0.1 \times 2.3 \times 198$ $= -68.3 \text{ kN}$ $M_2 = -68.3 \text{ kN}$ $M_3 = 1.5 \times 0.1 \times 2.3 \times 198$ $= 68.31 \text{ kN}$ $M_4 = 68.31 \text{ kN}$	$M_1 = -1.3 \times 0.1 \times 2.3 \times 198$ $= -59.2 \text{ kN}$ $M_2 = -59.2 \text{ kN}$ $M_3 = +1.3 \times 0.1 \times 2.3 \times 198$ $= 59.2 \text{ kN}$ $M_4 = 59.2 \text{ kN}$
About axis (1-1)	Combination 1	Combination 2
1) $M_1 = -(\sqrt{2} M_{ok}) - (\sqrt{2} M_{ok}) + (\sqrt{2} \times 0.1B \times V_{ok})$ 2) $M_2 = \sqrt{2} M_{ok} + \sqrt{2} M_{ok} - \sqrt{2} \times 0.1B \times V_{ok}$ 3) $M_3 = M_2$ 4) $M_4 = M_1$	$M_1 = -1 \times 58 - 0 \times 52 + 1.5 \times 0.1 \times 2.3 \times 198$ $M_1 = 10.31 \text{ kN}$ $M_2 = -10.31 \text{ kN}$ $M_3 = -10.31 \text{ kN}$ $M_4 = 10.31 \text{ kN}$	$M_1 = -1 \times 58 - 0 \times 52 + 1.3 \times 0.1 \times 2.3 \times 198$ $= 1.2 \text{ kN}$ $M_2 = +1 \times 58 - 0 \times 52 - 1.3 \times 0.1 \times 2.3 \times 198$ $= -1.2 \text{ kN}$ $M_3 = -1.2 \text{ kN}$ $M_4 = 1.2 \text{ kN}$

Maximum moments about B-B axis

$$M_d(B-B) = \begin{bmatrix} 68.31 \\ 59.2 \end{bmatrix} \text{ kN}$$

Maximum moments about 1-1 axis

$$M_d(1-1) = \begin{bmatrix} 10.31 \\ 1.2 \end{bmatrix} \text{ kN}$$

Effective footing area based on load combination 1&2

$$e_{(B-B)} = \begin{bmatrix} \frac{M_d(B-B)}{V_d} \\ \frac{68.31}{1826.24} \\ \frac{59.2}{1390.17} \\ 0.037 \\ 0.043 \end{bmatrix} \text{ m}$$

$\therefore e_{(B-B)} < \frac{B}{6}$ $\left[\because \frac{B}{6} = \frac{2.3}{6} = 0.38 \right]$ Hence ok.

Similarly,

$$e_{(1-1)} = \begin{bmatrix} \frac{M_d(1-1)}{V_d} \\ \frac{10.31}{1826.24} \\ \frac{1.2}{1390.17} \\ 0.0056 \\ 0.0009 \end{bmatrix}$$

$\therefore e_{(1-1)} < \frac{B}{6}$ $\left[\because \frac{B}{6} = 0.38 \right]$ Hence ok.

About B-B axis

About 1-1 axis

* Effective lengths and widths = (length and width in the direction of eccentricity - 2 x eccentricity)

$$\begin{aligned} & \left[\begin{array}{l} (2.3 - 0.037) - 2 \times 0.037 \\ (2.3 - 0.043) - 2 \times 0.043 \end{array} \right] \\ & = \left[\begin{array}{l} 2.19 \\ 2.7 \end{array} \right] \end{aligned}$$

$$\begin{aligned} & \left[\begin{array}{l} (2.3 - 0.0058) - 2 \times 0.0058 \\ (2.3 - 0.0009) - 2 \times 0.0009 \end{array} \right] \\ & = \left[\begin{array}{l} 2.28 \\ 2.30 \end{array} \right] \end{aligned}$$

* Smaller effective dimensions $A' = L' \times B'$

$$= \left[\begin{array}{l} 4.8 \\ 4.71 \end{array} \right]$$

$$\left[\begin{array}{l} 5.2 \\ 5.29 \end{array} \right]$$

* Q_{design}

$$Q_{Ed} = \frac{V_d}{d1}$$

$$= \left[\begin{array}{l} \frac{1826.24}{4.8} \\ \frac{1390.17}{4.71} \end{array} \right]$$

$$\left[\begin{array}{l} \frac{1826.24}{5.2} \\ \frac{1390.17}{4.71} \end{array} \right]$$

$$= \left[\begin{array}{l} 380.47 \\ 295.15 \end{array} \right]$$

$$= \left[\begin{array}{l} 351.2 \\ 262.79 \end{array} \right]$$

Bearing capacity (undrained condition)

$$Q_{ult} = (\pi + 2) C_u b_c s_c i_c + q$$

$$C_u = \text{SPT value} \times 5$$

$$= 2 \times 5 = 100$$

	About axis B-B	About (1-1)
1) undrained strength (C_u)	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$
2) $C_u / \gamma C_u$	$\begin{bmatrix} 100 / 1 \\ 100 / 1.4 \end{bmatrix} = \begin{bmatrix} 100 \\ 71.43 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 71.43 \end{bmatrix}$
3) $b_c = \frac{1 - 2\alpha}{\pi + 2}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
4) $s_c = 1.2$ for square or circular footing	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$
5) $i_c = 0.5 \left(1 + \sqrt{1 - \frac{H}{\lambda C_u}} \right)$ provided $H \leq \lambda C_u$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
6) γ = density of soil x depth of footing	$\begin{bmatrix} 18 \times 3 = 54 \\ 18 \times 3 = 54 \end{bmatrix} \text{ kNm}$	$\begin{bmatrix} 18 \times 3 = 54 \\ 18 \times 3 = 54 \end{bmatrix} \text{ kNm}$
7) $Q_{ult} = (\pi + 2) C_u b_c s_c i_c + q$	$\begin{bmatrix} (\pi + 2) \times 100 \times 1 \times 1.2 \times 1 + 5.4 \\ (\pi + 2) \times 100 \times 1 \times 1.2 \times 1 + 5.4 \end{bmatrix}$ $= \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix} \text{ kPa}$	similarly, $= \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix} \text{ kPa}$
8) $Q_{ult} / \gamma R$	$\begin{bmatrix} 670.8 / 1 \\ 494.58 / 1 \end{bmatrix} = \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$
9) utilization factor	$\begin{bmatrix} \frac{380.47}{670.8} \times 100 \\ \frac{295.15}{494.58} \times 100 \end{bmatrix}$ $= \begin{bmatrix} 56.72\% \\ 59.68\% \end{bmatrix} < 100\%$	$\begin{bmatrix} \frac{351.2}{670.8} \times 100 \\ \frac{262.79}{494.58} \times 100 \end{bmatrix}$ $= \begin{bmatrix} 52.35\% \\ 53.13\% \end{bmatrix} < 100\%$

	About axis (B-B)	About axis (1-1)
* $M = \frac{U}{B}$	$\begin{bmatrix} \frac{2.17}{2.17} \\ \frac{2.17}{2.17} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} \frac{2.28}{2.28} \\ \frac{2.3}{2.3} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$
* $N = \frac{H}{B}$ [$\because H = 4 \times B$]	$\begin{bmatrix} \frac{4 \times 2.3}{2.17} \\ \frac{4 \times 2.3}{2.17} \end{bmatrix} = \begin{bmatrix} 4.2 \\ 4.24 \end{bmatrix}$	$\begin{bmatrix} \frac{4 \times 2.3}{2.28} \\ \frac{4 \times 2.3}{2.3} \end{bmatrix} = \begin{bmatrix} 4.03 \\ 4 \end{bmatrix}$

$$E_s = 100 \times \frac{Q_{uni}}{2}$$

$$Q_{uni} = 2 \times C_u$$

$$= 2 \times 5 \times \text{SPT value} \quad [\because C_u = 5 \times \text{SPT value}]$$

$$E_s \text{ at } 3.5 = 1000 \times 5 \times 20 = 1,00,000 \text{ kpc}$$

$$E_s \text{ at } 5.5 = 1000 \times 5 \times 54 = 2,50,000 \text{ kpc}$$

$$E_s \text{ at } 8.0 = 1000 \times 5 \times 80 = 2,50,000 \text{ kpc}$$

$$E_s \text{ (weighted average)} = \frac{1,00,000 \times 3.5 + 2,50,000 \times 5.5 + 2,50,000 \times 8.0}{12} = 22382 \text{ kpc}$$

$$A_H = q_0 B^1 \times \frac{1-M^2}{E_s} \left(I_1 + \frac{1-2M}{1-M} I_2 \right) I_F$$

$$I_1 = \frac{1}{\pi} \left[M \times \ln \frac{(1 + \sqrt{1+m^2} \sqrt{M^2+N^2})}{M (1 + \sqrt{M^2+N^2+1})} + \ln \frac{(M + \sqrt{M^2+1} \sqrt{1+N^2})}{(M + \sqrt{M^2+N^2+1})} \right]$$

$$I_2 = \frac{N}{2\pi} \tan^{-1} \left[\frac{M}{N \sqrt{M^2+N^2+1}} \right]$$

- About B-B axis :

Combination 1:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.2)^2}}{1 + \sqrt{1^2 + (4.2)^2 + 1}} + \ln \frac{(1 + \sqrt{1^2 - 1}) \sqrt{1 + (4.2)^2}}{1 + \sqrt{1^2 + (4.2)^2 + 1}} \right]$$

$$= 0.419$$

$$I_2 = \frac{4.2}{2\pi} \tan^{-1} \left(\frac{1}{4.2 \sqrt{1^2 + (4.2)^2 + 1}} \right) = ~~0.419~~ 2.06$$

$$\Delta_H = 280.47 \times 2.19 \times \frac{1-0.3^2}{22382} \left[0.42 + \frac{1.2 \times 0.3}{1-0.3} \times 2.06 \right] \times 0.632$$

$$= 0.0003419$$

To limit settlement to 50 mm $q = \frac{0.05}{0.0003419} = 158.78 \text{ kN/m}^2$

Combination 2:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.24)^2}}{1(1 + \sqrt{1^2 + (4.24)^2 + 1})} + \ln \frac{(1 + \sqrt{1^2 - 1}) \sqrt{1^2 + (4.24)^2}}{1(1 + \sqrt{1^2 + (4.24)^2 + 1})} \right]$$

$$= 0.42$$

$$I_2 = \frac{4.24}{2\pi} \tan^{-1} \left(\frac{1}{4.24 \sqrt{1^2 + (4.24)^2 + 1}} \right) = 2.04$$

$$\Delta_H = 295.15 \times 2.17 \times \frac{1-0.3^2}{22382} \left[0.42 + \frac{1.2 \times 0.3}{1-0.3} \times 2.04 \right] \times 0.632$$

$$= 0.000164$$

- To limit settlement to 50 mm $q = \frac{0.05}{0.000164} = 304.87 \text{ kN/m}^2$

About t-1 axis

Combination 1 :-

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2+1}) \sqrt{1^2+(4.03)^2}}{(1 + \sqrt{1^2+(4.03)^2+1})} + \ln \frac{(1 + \sqrt{1^2+1}) \sqrt{1+(4.03)^2}}{1 + \sqrt{1^2+(4.03)^2+1}} \right]$$
$$= 0.41$$

$$I_2 = \frac{4.03}{2\pi} \tan^{-1} \left[\frac{1}{(4.03) \sqrt{1^2+(4.03)^2+1}} \right] = 2.13$$

$$\Delta_H = 351.2 \times 2.28 \times \frac{1-0.3^2}{2 \times 3 \times 2} \left[0.41 + \frac{1-2 \times 0.3}{1-0.3} \times 2.13 \right] \times 0.632$$
$$= 0.000348$$

To limit settlement to 50mm $\sigma = \frac{0.05}{0.000348}$

$$= 143.68 \text{ kN/m}^2$$

Combination 2:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2+1}) \sqrt{1^2+4^2}}{(1 + \sqrt{1^2+(4)^2+1})} + \ln \frac{(1 + \sqrt{1^2+1}) \sqrt{1+4^2}}{1 + \sqrt{1^2+4^2+1}} \right]$$
$$= 0.41$$

$$I_2 = \frac{4}{2\pi} \tan^{-1} \left[\frac{1}{(4) \sqrt{1^2+4^2+1}} \right] = 2.15$$

$$\Delta_H = 26 \times 2.79 \times 2.3 \times \frac{1-0.3^2}{2 \times 3 \times 2} \left[0.41 + \frac{1-2 \times 0.3}{1-0.3} \times 2.15 \right] \times 0.632$$
$$= 0.0001746$$

To limit settlement to 50mm $\sigma = 286.36 \text{ kN/m}^2$

iv) Design of B_2 pad footing:

The assigned parameters for footing B_2

Vertical load (dead load) $V_{Gk} = 319 \text{ kN}$

Vertical live load (V_{Qk}) = 99 kN

V_{Gk} eccentricity = 0 both ways

V_{Qk} eccentricity = $0.1 B$ both ways

Moment due to D.L (M_{Gk}) for axis 2-2 = 69 kNm

Moment due to L.L (M_{Qk}) for axis 2-2 = 46 kNm

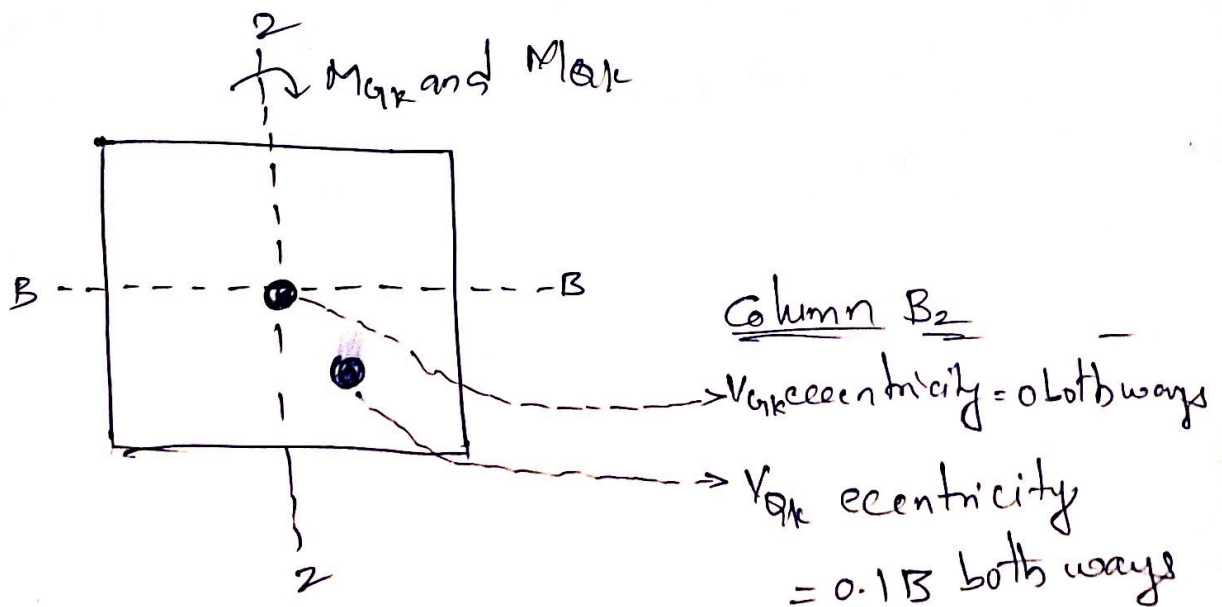
Unit weight of concrete = 25 kN/m^3

unit weight of soil = 18 kN/m^3

Thickness of footing = 0.3 m

Depth = 3 m

Column B_2 :-



let assume pad length & width to be 2.3 m (2)

$$\Rightarrow \text{self weight } (W_{GK}) = 2.3 \times 2.3 \times 0.3 \times 25 \\ = 39.68 \text{ kN}$$

$$\Rightarrow \text{Dead load } (B_{GK}) = (3 - 0.3) \times 2.3 \times 2.3 \times 18 \\ = 257.09 \text{ kN}$$

* partial factors for design loads -

Combination 1

$$\gamma_{G1} = 1.35$$

$$\gamma_{Q1} = 1.5$$

$$\gamma_{Q1, \text{fav}} = 0$$

Combination 2

$$\gamma_{G2} = 1.0$$

$$\gamma_{Q2} = 1.3$$

$$\gamma_{Q2, \text{fav}} = 0$$

$$\rightarrow \text{Total } V_{GK} = W_{GK} + B_{GK} + V_{GK}(\text{given}) \\ = 39.68 + 257.09 + 319 \\ = 615.77 \text{ kN}$$

also

$$V_d = \begin{bmatrix} \text{Combination 1} \\ \text{Combination 2} \end{bmatrix} = \begin{bmatrix} \gamma_{G1} (\text{total } V_{GK}) + (\gamma_{Q1} \times V_{QK}) - \gamma_{Q1, \text{fav}} \times V_{QKb} \\ \gamma_{G2} (\text{total } V_{GK}) + (\gamma_{Q2} \times V_{QK}) - \gamma_{Q2, \text{fav}} \times V_{QKb} \end{bmatrix} \\ = \begin{bmatrix} 1.35 (615.77) + 1.5 \times 99 - 0 \\ 1.0 \times (615.77) + 1.3 \times 99 - 0 \end{bmatrix} \\ = \begin{bmatrix} 979.47 \\ 744.47 \end{bmatrix} \text{ kN}$$

Design moments based on load combination 1 & 2

* calculation of moments on quadrant I, II, III, IV w.r.t axis (A-B) and axis (2-2)

about axis (2-2)	Combination 1	Combination 2
$1) M_1 = -\gamma_{G, fav} \times M_{GK} - \gamma_{Q, fav} \times M_{QK}$ $- (\gamma_{Q, unfav} \times 0.1B \times V_{QK})$	$= -1 \times 69 - 0 \times 46$ $- (1.5 \times 0.1 \times 2.3 \times 99)$ $M_1 = -103.16$	$= -1 \times 69 - 0 \times 46$ $- (1.3 \times 0.1 \times 2.5 \times 99)$ $M_1 = \cancel{202.40} - 98.6$
$2) M_2 = \gamma_{G, fav} (M_{GK}) + \gamma_{Q, fav} M_{QK}$ $+ \gamma_{Q, unfav} \times 0.1B \times V_{QK}$	$M_2 = 1 \times 69 + 0 \times 46$ $+ (1.5 \times 0.1 \times 2.3 \times 99)$ $= 103.16$	$M_2 = 1 \times 69 + 0 \times 46$ $+ 1.3 \times 0.1 \times 2.5 \times 99$ $M_2 = 98.6$
$3) M_3 = M_2$	$M_3 = 103.16$	$M_3 = M_2 = 98.6$
$4) M_4 = M_1$	$M_4 = -103.16$	$M_4 = -98.6$
about axis (B-B)	Combination 1	Combination 2
$1) M_1 = 0 + 0 - (\gamma_{Q, unfav} \times 0.1B \times V_{QK})$	$M_1 = -(1.5 \times 0.1 \times 2.3 \times 99)$ $= -34.155$	$M_1 = 1.3 \times 0.1 \times 2.3 \times 99$ $= 29.6$
$2) M_2 = M_1$	$M_2 = -34.155$	$M_2 = 29.6$
$3) M_3 = 0 + 0 + (\gamma_{Q, unfav} \times 0.1B \times V_{QK})$	$M_3 = 1.5 \times 0.1 \times 2.3 \times 99$ $= 34.155$	$M_3 = 1.3 \times 0.1 \times 2.3 \times 99$ $= 29.6$
$4) M_4 = M_3$	$M_4 = 34.155$	$M_4 = 29.6$

Maximum moment about B-B axis

(20)

$$M_d(B-B) = \begin{bmatrix} 34.155 \\ 29.6 \end{bmatrix} \text{ kN}$$

Maximum moment about 2-2 axis

$$M_d(2-2) = \begin{bmatrix} 103.16 \\ 98.6 \end{bmatrix} \text{ kN}$$

Effective footing area based on load combination 1 of 2

$$e_{(B-B)} = \begin{bmatrix} \frac{M_d(B-B)}{V_d} \\ \frac{34.155}{979.79} \\ \frac{29.6}{744.42} \\ 0.035 \\ 0.04 \end{bmatrix} \text{ m}$$

$$\therefore e_{(B-B)} < \frac{B}{6} \text{ Hence ok } \left[\because \frac{B}{6} = \frac{2.3}{6} = 0.38 \right]$$

Similarly,

$$e_{(2-2)} = \begin{bmatrix} \frac{M_d(2-2)}{V_d} \\ \frac{103.16}{979.79} \\ \frac{98.6}{744.42} \\ 0.11 \\ 0.13 \end{bmatrix}$$

$$\therefore e_{(2-2)} < \frac{B}{6} \text{ Hence ok}$$

-About ~~B~~-B axis

-About 2-2 axis

* Effective length and width = (length and width in the direction of eccentricity) \div $2 \times$ eccentricity

* smaller effective dimension $A' = L' \times B'$

* a design
$$Q_{Ed} = \frac{V_d}{A'}$$

$$\begin{bmatrix} (2.3 - 0.035) - 2 \times 0.035 \\ (2.3 - 0.04) - 2 \times 0.04 \end{bmatrix}$$

$$\begin{bmatrix} 2.195 \\ 2.18 \end{bmatrix}$$

$$= \begin{bmatrix} 4.82 \\ 4.75 \end{bmatrix}$$

$$\begin{bmatrix} \frac{979.77}{4.82} \\ \frac{744.42}{4.75} \end{bmatrix}$$

$$\begin{bmatrix} 203.28 \\ 156.73 \end{bmatrix}$$

$$\begin{bmatrix} (2.3 - 0.11) - 2 \times 0.11 \\ (2.3 - 0.13) - 2 \times 0.13 \end{bmatrix}$$

$$\begin{bmatrix} 1.97 \\ 1.91 \end{bmatrix}$$

$$\begin{bmatrix} 3.88 \\ 3.65 \end{bmatrix}$$

$$\begin{bmatrix} \frac{979.77}{3.88} \\ \frac{744.42}{3.65} \end{bmatrix}$$

$$\begin{bmatrix} 252.52 \\ 203.96 \end{bmatrix}$$

Bearing capacity (undrained condition)

$$Q_{ult} = (\pi + 2) C_u b c_s c_f c_d + q$$

$$C_u = \text{SPT value} \times 5$$

$$= 20 \times 5 = 100$$

	About axis B-B	About axis (2-2)
1) undrained strength (C_u)	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 100 \end{bmatrix}$
2) $\frac{C_u}{\sqrt{C_u}}$	$\begin{bmatrix} 100/1 \\ 100/1.4 \end{bmatrix} = \begin{bmatrix} 100 \\ 71.43 \end{bmatrix}$	$\begin{bmatrix} 100 \\ 71.42 \end{bmatrix}$
3) $b_c = \frac{1-2\alpha}{\pi+2}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
4. $S_c = 1.2$ for square or circular footing	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$	$\begin{bmatrix} 1.2 \\ 1.2 \end{bmatrix}$
5. $P_c = 0.5 \left(1 + \sqrt{1 - \frac{H}{\lambda C_u}}\right)$ provided $H \leq \lambda C_u$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 1 \end{bmatrix}$
6. $q =$ density of soil \times depth of footing	$\begin{bmatrix} 18 \times 30 = 54 \\ 18 \times 3 = 54 \end{bmatrix}$ kNm	$\begin{bmatrix} 54 \\ 54 \end{bmatrix}$ kNm
7. $Q_{ult} = (\pi + 2) C_u b c_s c_f c_d + q$	$\begin{bmatrix} (\pi + 2) \times 100 \times 1 \times 1.2 \times 1 + 54 \\ (\pi + 2) \times 71.42 \times 1 \times 1.2 \times 1 + 54 \end{bmatrix}$ $= \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$ kPa
8. Q_{ult} / γ	$\begin{bmatrix} 670.8/1 \\ 494.58/1 \end{bmatrix} = \begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$	$\begin{bmatrix} 670.8 \\ 494.58 \end{bmatrix}$
9. utilization factor $= \frac{Q_{ed}}{Q_{ult}} \times 100$	$\begin{bmatrix} 203.28 / 670.8 \times 100 \\ 156.73 / 494.58 \times 100 \end{bmatrix} = \begin{bmatrix} 30.3\% \\ 31.6\% \end{bmatrix}$ $< 100\%$	$\begin{bmatrix} 252.52 / 670.8 \times 100 \\ 203.9 / 494.58 \times 100 \end{bmatrix} = \begin{bmatrix} 37.6\% \\ 41.2\% \end{bmatrix}$ $< 100\%$ Hence ok

	About axis B-B	About axis z-z
* $M = \frac{L}{B}$	$\begin{bmatrix} \frac{2.195}{2.195} \\ \frac{2.18}{2.18} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} \frac{1.97}{1.97} \\ \frac{1.97}{1.97} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$
* $N = \frac{H}{B}$ ($\because H = u \times B$)	$\begin{bmatrix} \frac{4 \times 2.3}{2.195} \\ \frac{4.23}{2.18} \end{bmatrix} = \begin{bmatrix} 4.19 \\ 4.22 \end{bmatrix}$	$\begin{bmatrix} \frac{4 \times 2.3}{1.97} \\ \frac{4 \times 2.3}{1.97} \end{bmatrix} = \begin{bmatrix} 4.67 \\ 4.82 \end{bmatrix}$

$E_s = 1000 \times Q_{uni} / 2$

$Q_{uni} = 2 \times C_u$ [$\because C_u = 5 \times \text{SPT value}$]
 $= 2 \times 5 \times \text{SPT value}$

E_s at 3.5 m = $1000 \times 5 \times 20 = 100000 \text{ kPa}$

E_s at 5.5 m = $1000 \times 5 \times 54 = 270,000 \text{ kPa}$

E_s at 8.0 m = $1000 \times 5 \times 100 = 2,50,000 \text{ kPa}$

E_s (weighted average) = $\frac{100000 \times 3.5 + 270,000 \times 5.5 + 2,50,000 \times 8.0}{10}$
 $= 22382 \text{ kPa}$

$A_H = 20 B' \times \frac{1-M^2}{E_s} \left(I_1 + \frac{1-2M}{1-M} I_2 \right) I_F$

$I_1 = \frac{1}{\pi} \left[M \times \ln \frac{(1 + \sqrt{1+m^2} \sqrt{m^2+N^2})}{M(1 + \sqrt{M^2+N^2+1})} + \ln \frac{(M + \sqrt{M^2+1}) \sqrt{1+N^2}}{(M + \sqrt{M^2+N^2+1})} \right]$

$I_2 = \frac{N}{2\pi} \tan^{-1} \left[\frac{M}{N \sqrt{M^2+N^2+1}} \right]$

About B-B axis

Combination 1:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.19)^2}}{1(1 + \sqrt{1^2 + (4.19)^2 + 1})} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (4.19)^2}}{1 + \sqrt{1^2 + (4.19)^2 + 1}} \right]$$

$$= 0.41$$

$$I_2 = \frac{4.19}{2\pi} \tan^{-1} \left(\frac{1}{4.19 \sqrt{1^2 + (4.19)^2 + 1}} \right) = 2.06$$

$$\Delta_4 = 203.28 \times 2.195 \times \frac{1 - 0.3^2}{22382} \left[0.41 + \frac{1 - 0.3 \times 0.2}{1 - 0.3} \times 2.06 \right] \times 0.623$$
$$= 0.00133$$

To limit settlement to 50mm $q = 375 \text{ kN/m}^2$

Combination 2

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.22)^2}}{1(1 + \sqrt{1^2 + (4.22)^2 + 1})} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (4.22)^2}}{1(1 + \sqrt{1^2 + (4.22)^2 + 1})} \right]$$
$$= 0.42$$

$$I_2 = \frac{4.22}{2\pi} \tan^{-1} \left(\frac{1}{4.22 \sqrt{1^2 + (4.22)^2 + 1}} \right) = 2.05$$

$$\Delta_4 = 202.156.73 \times 2.18 \times \frac{1 - 0.3^2}{22382} \left[0.42 + \frac{1 - 2 \times 0.3}{1 - 0.3} \times 2.05 \right] \times 0.623$$
$$=$$
$$= 0.000138$$

To limit settlement to 50mm $q = 362.31 \text{ kN/m}^2$

About 2-2 axis

Combination 1:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.67)^2}}{(1 + \sqrt{1^2 + (4.67)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (4.67)^2}}{1 + \sqrt{1^2 + (4.67)^2} + 1} \right]$$
$$= 0.43$$

$$I_2 = \frac{4.67}{2\pi} \tan^{-1} \left(\frac{1}{4.67 \sqrt{1^2 + (4.67)^2} + 1} \right) = 1.87$$

$$\Delta_H = 252.52 \times 1.97 \times \frac{1 - 0.3^2}{22882} \times \left[0.43 + \frac{1 - 2 \times 0.3}{1 - 0.3} \times 1.87 \right] \times 0.632$$
$$= 0.0001915$$

To limit settlement to 50mm $q = 263.15$

Combination 2:

$$I_1 = \frac{1}{\pi} \left[1 \times \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + (4.82)^2}}{(1 + \sqrt{1^2 + (4.82)^2} + 1)} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + (4.82)^2}}{1 + \sqrt{1^2 + (4.82)^2} + 1} \right]$$
$$= 0.43$$

$$I_2 = \frac{4.82}{2\pi} \tan^{-1} \left(\frac{1}{4.82 \sqrt{1^2 + (4.82)^2} + 1} \right) = 1.82$$

$$\Delta_H = 203.9 \times 1.97 \times \frac{1 - 0.3^2}{22362} \times \left[0.43 + \frac{1 - 2 \times 0.3}{1 - 0.3} \times 1.82 \right] \times 0.682$$
$$= 0.00014627$$

To limit settlement to 50mm $q = 341.83 \text{ kN/m}^2$

2)

Design of Raft footing

①

* Dimensions of Raft foundation,

Length = 22.4 m

width = 12.4 m

Thickness = 0.75 m

— Area = $22.4 \times 12.4 = 277.76 \text{ m}^2$

Yield strength = 400 MPa

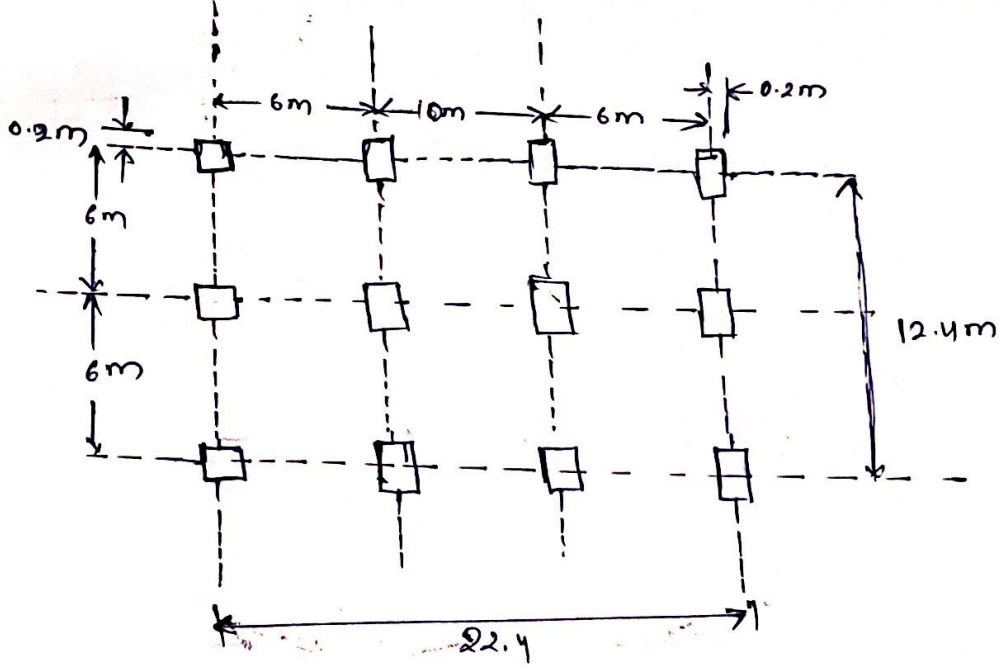
Concrete cover = 50 mm

Concrete clamps = 30

* Given parameter values of column A_1, A_2, B_1, B_2 are :-

	A_1	A_2	B_1	B_2
V_{4k}	455	314	836	319
V_{9k}	273	73	198	99

	V_{4k}	V_{9k}
$A_1 = A_4 = C_1 = C_4$	$4 \times 455 = 1820$	$4 \times 273 = 1092$
$A_2 = A_3 = C_2 = C_3$	$4 \times 314 = 1256$	$4 \times 73 = 292$
$B_1 = B_4$	$2 \times 836 = 1672$	$2 \times 198 = 396$
$B_2 = B_3$	$2 \times 319 = 638$	$2 \times 99 = 198$
Total	5386	2786 1978



Self weight of raft = $22.4 \times 12.4 \times 0.75 \times 25$

$w_{GK} = 5208 \text{ kN/m}$

Permanent actions = self weight of raft (w_{GK}) + ~~Total~~ $\sum V_{GK}$ (all actions)

= $5208 + 5386$

\therefore Total $V_{GK} = 10594$

\therefore Total $V_{QK} = 1978$

Total factored load as per combinations 1 & 2

$$V_d = \begin{bmatrix} 1.35(w_{GK} + V_{GK}) + 1.5 V_{QK} \\ 1(w_{GK} + V_{GK}) + 1.3 V_{QK} \end{bmatrix}$$

$$= \begin{bmatrix} 1.35(10594) + 1.5(1978) \\ 1(10594) + 1.3(1978) \end{bmatrix}$$

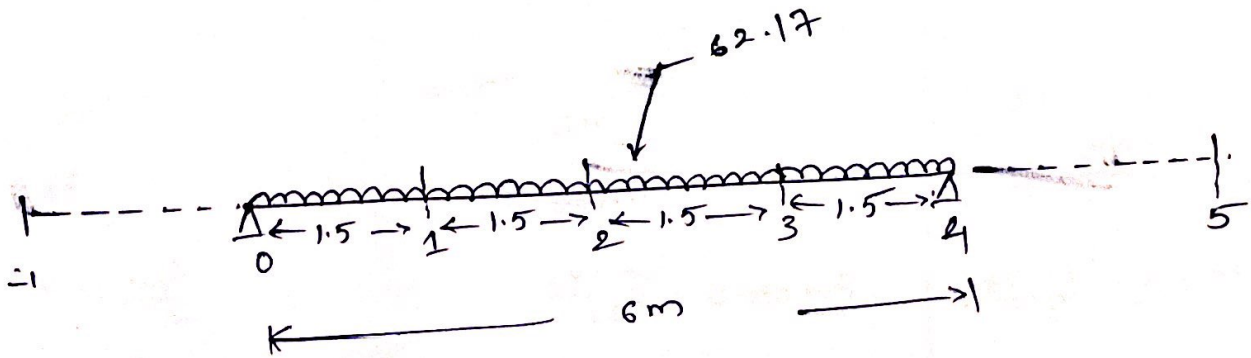
$$V_d = \begin{bmatrix} 18483.9 \\ 14218.4 \end{bmatrix} \text{ kN} = \begin{bmatrix} 17268.7 \\ 13165.4 \end{bmatrix} \text{ kN}$$

∴ Factored based on the $\gamma_d = \frac{\text{Total factored load}}{\text{Area of raft}}$ (3)

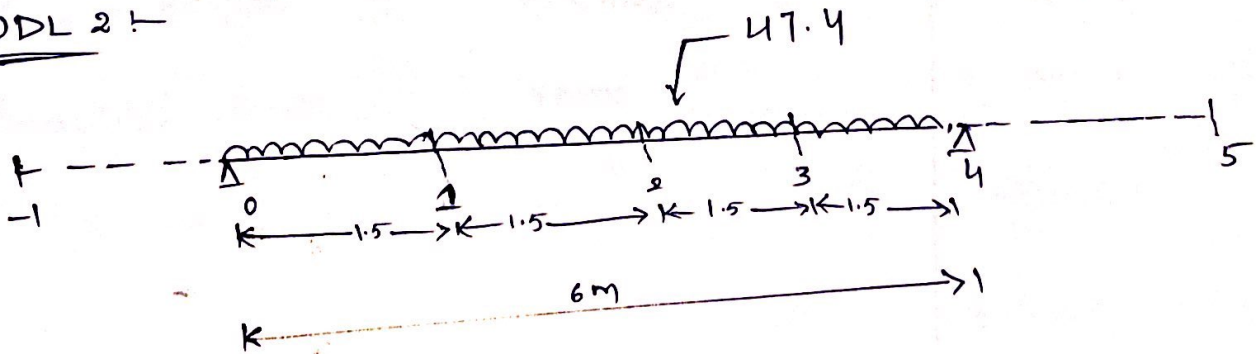
$$UDL_{1+2} = \left[\begin{array}{c} 17268.9 \\ 277.76 \\ 13165.4 \\ 277.76 \end{array} \right] \text{ kN/m}^2$$

$$= \left[\begin{array}{c} 62.17 \\ 47.4 \end{array} \right] \text{ kN/m}^2$$

UDL 1



UDL 2



Combination 1

Combination 2

1. $V_d = \gamma_g \times \text{total } V_{gk} + \gamma_q \times \text{total } V_{qk}$

$= 1.35 \times 10594 + 1.5 \times 1978$
 $= 17268.9 \text{ kN}$

$= 1.0 \times 10594 + 1.3 \times 1978$
 $= 13165.4 \text{ kN}$

2. $Q_{design}(Q_{Ed}) = \frac{V_d}{A}$

$\frac{17268.9}{277.76} = 62.17 \text{ kN/m}^2$

$\frac{13165.4}{277.76} = 47.4 \text{ kN/m}^2$

3. Type of soil
 k (0.3 x 0.3)

clay (25,000 kN/m³)

clay (25,000 kN/m³)

4. $k_s = k_{(0.3 \times 0.3)} \left[\frac{\frac{L}{B} + 0.5}{1.5 \frac{L}{B}} \right]$

$= 25,000 \left[\frac{\frac{22.4}{12.4} + 0.5}{1.5 \times \frac{22.4}{12.4}} \right] = 21296.29 \text{ kN/m}^3$

$= 25000 \left[\frac{\frac{22.4}{12.4} + 0.5}{1.5 \times \frac{22.4}{12.4}} \right] = 21296.29 \text{ kN/m}^3$

5. b

4m

4m

6. d

0.75m

0.75m

7. $I = \frac{bd^3}{12}$

$\frac{4 \times 0.75^3}{12} = 0.035 \text{ m}^4$

$\frac{4 \times 0.75^3}{12} = 0.035 \text{ m}^4$

8. $f_{cm} = 33 \text{ MPa}$

33 MPa

33 MPa

9. $E_{cm} [\text{MPa}] = 22000$

22,000

22000

10. $[f_{tm} / 10 \text{ MPa}]$

31475.8

31475.8

11. E

31475806 kN/m²

31475806 kN/m²

12. $h = \frac{L}{4}$

$\frac{6}{4} = 1.5 \text{ m}$

$\frac{6}{4} = 1.5 \text{ m}$

13. $h^4 \frac{E}{EI}$

$\frac{1.5^4}{31475806 \times 0.035} = 0.00000459 \text{ m}^2$

$\frac{1.5^4}{31475806 \times 0.035} = 0.00000459 \text{ m}^2$

14. $\frac{2h^4}{EI}$

$\frac{62.17 \times 1.5^4}{31475806 \times 0.035} = 0.000285 \text{ kN}$

$\frac{47.4 \times 1.5^4}{31475806 \times 0.035} = 0.000285$

15. $\frac{k h^4}{EI}$

$\frac{21296.29 \times 1.5^4}{31475806 \times 0.035} = 0.0978 \text{ kN/m}$

$= 0.0978 \text{ kN/m}$

Combination 1

Combination 2

5

$$16. y_2 = \frac{\left(\frac{qh^4}{EI}\right) \left(1 + \frac{8}{(6+kh^4/EI)}\right)}{\left(6 + \frac{kh^4}{EI}\right) - \left(\frac{32}{6+kh^4/EI}\right)}$$

$$0.000286 \left[1 + \frac{8}{6+0.0978}\right]$$

$$\frac{\left[6+0.0978\right] - \left[\frac{32}{6+0.0978}\right]}{6+0.0978}$$

$$= 0.000778 \text{ m}$$

$$0.000218 \left[1 + \frac{8}{6+0.09786}\right]$$

$$\frac{\left[6+0.09786\right] - \left[\frac{32}{6+0.09786}\right]}{6+0.09786}$$

$$= 0.000593 \text{ m}$$

$$17. y_1 = \frac{y_2 \left(6 + \frac{kh^4}{EI}\right) - \left(\frac{qh^4}{EI}\right)}{8}$$

$$= \frac{0.000778(6+0.0978) - (0.000286)}{8}$$

$$= 0.000557 \text{ m}$$

$$= \frac{0.000593(6+0.09786) - (0.000218)}{8}$$

$$= 0.000425 \text{ m}$$

$$18. y_1 = \frac{\frac{qh^4}{EI} + 4y_2}{\left(6 + \frac{kh^4}{EI}\right)}$$

$$= \frac{(0.000286) + 4 \times 0.000778}{6+0.0978}$$

$$= 0.000557 \text{ m}$$

$$= \frac{(0.000218) + 4 \times 0.000593}{6+0.0978}$$

$$= 0.000425 \text{ m}$$

19. y_2

0.77 mm

0.59 mm

20. $y_1 = y_3$

= 0.55 mm

0.42 mm

21. $y_{L1} = y_{R1} = -y_1$

-0.55 mm

-0.42 mm

23. $y_2 = y_4$

0

0

Bearing capacity (undrained condition)

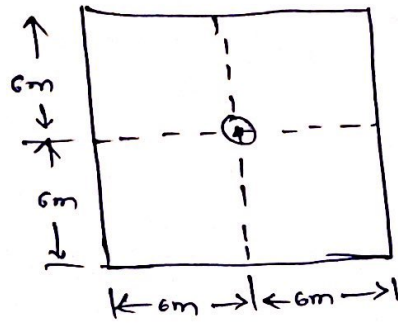
$$Q_{ult} = (\pi + 2) c_u b_c s_c p_c + q$$

$$c_u = \text{SPT value} \times 5$$

$$= 26 \times 5 = 130$$

	Combination 1	Combination 2
1) undrained strength (c_u)	130	130
2. $c_u A_{cu}$	$\frac{130}{1} = 130$	$\frac{130}{1.4} = 92.85$
3. $b_c = 1 - \frac{2e}{(\pi + 2)}$	1	1
4. s_c	1.1	1.01
5. p_c	1	1
6. $q = \text{density of soil} \times \text{depth of footing}$	$18 \times 0.75 = 13.50 \text{ kN/m}^2$	13.50 kN/m^2
7. $Q_{ult} = (\pi + 2) c_u b_c s_c p_c + q$	$(\pi + 2) \times 130 \times 1 \times 1.1 \times 1 + 13.5$ $= 755.91 \text{ kN/m}^2$	$(\pi + 2) \times 92.85 \times 1 \times 1.01 \times 1 + 13.5$ 496.67 kN/m^2
8. utilization ($\frac{Q_{ult}}{Q_{req}}$)	$\frac{755.91}{1} = 755.91$	$\frac{496.67}{1} = 496.67$
9. utilization ratio $\frac{Q_{ed}}{Q_{ult}} \times 100$	$\frac{62.17}{755.91} \times 100 = 8.23\%$	$\frac{47.4}{496.67} \times 100 = 9.54\%$
	$< 100\%$	$< 100\%$

settlement check combination 1 & 2



Combination 1

Combination 2

$$M = \frac{L}{B}$$

$$\frac{6}{6} = 1$$

$$\frac{6}{6} = 1$$

$$N = \frac{H}{B}$$

$$\frac{15}{6} = 2.5$$

$$\frac{15}{6} = 2.5$$

$$H \leq H \times B$$

$$15 \text{ m}$$

$$15 \text{ m}$$

$$E_s = 1000 \times \frac{Q_{unif}}{2}$$

$$Q_{unif} = 2 \times E_u$$

$$= 5 \times \text{spt value} \times 2$$

$$E_s = \frac{1000 \times 2 \times 5 \times \text{SPT value}}{2}$$

$$E_s \text{ at } 2.0 \text{ m} = 1000 \times 5 \times 26 = 130000 \text{ kPa}$$

$$E_s \text{ at } 3.0 \text{ m} = 1000 \times 5 \times 23 = 115000 \text{ kPa}$$

$$E_s \text{ at } 5.0 \text{ m} = 1000 \times 5 \times 20 = 100000 \text{ kPa}$$

$$E_s \text{ at } 6.0 \text{ m} = 1000 \times 5 \times 54 = 270000 \text{ kPa}$$

$$E_s \text{ at } 9.5 \text{ m} = 1000 \times 5 \times 50 = 250000 \text{ kPa}$$

$$E_s \text{ at } 11 \text{ m} = 1000 \times 5 \times 43 = 215000 \text{ kPa}$$

$$E_s \text{ at } 13 \text{ m} = 1000 \times 5 \times 59 = 295000 \text{ kPa}$$

$$E_s \text{ at } 15 \text{ m} = 1000 \times 5 \times 64 = 320000 \text{ kPa}$$

$$295000 \times 13 + 320000 \times 15$$

$$E_s \text{ weighted average} = \frac{130000 \times 2.0 + 115000 \times 3 + 100000 \times 5 + 270000 \times 6 + 250000 \times 9.5 + 215000 \times 11 + 295000 \times 13 + 320000 \times 15}{64.5}$$

$$I_1 = \frac{1}{\pi} \left(m \ln \frac{(1 + \sqrt{m^2 + 1}) \sqrt{m^2 + N^2}}{m (1 + \sqrt{m^2 + N^2 + 1})} + \ln \frac{(m \sqrt{m^2 + 1} + \sqrt{1 + N^2})}{M + \sqrt{m^2 + N^2 + 1}} \right)$$

For combination 1 & 2:

$$I_1 = \frac{1}{\pi} \left[1.0 \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1^2 + 2.5^2}}{1 + (1 + \sqrt{1^2 + 2.5^2 + 1})} + \ln \frac{(1 + \sqrt{1^2 + 1}) \sqrt{1 + 2.5^2}}{1 + \sqrt{1^2 + 2.5^2 + 1}} \right]$$

$$= 0.330$$

$$I_2 = \frac{N}{2\pi} \tan^{-1} \left(\frac{m}{N (\sqrt{m^2 + N^2 + 1})} \right)$$

$$= \frac{2.5}{2\pi} \tan^{-1} \left(\frac{1}{2.5 \sqrt{1^2 + 2.5^2 + 1}} \right)$$

$$= ~~0.08~~ 3.16$$

$$\frac{D}{B} = \frac{0.75}{12.40} = 0.060$$

$$\frac{L}{B} = \frac{22.40}{12.40} = 1.806$$

$$I_F = 0.980$$

$$\mu = 0.3$$

Combination 1:

$$Q = 755.91$$

$$\Delta_H = Q_0 B^1 \frac{1 - \mu^2}{E_s} \left(I_1 + \frac{1 - 2\mu}{1 - \mu} I_2 \right) I_F =$$

$$\Delta_H = 7.574 \text{ mm}$$

Combination 2:

$$Q = 496.67$$

$$\Delta_H = Q_0 B^1 \frac{1 - \mu^2}{E_s} \left(I_1 + \frac{1 - 2\mu}{1 - \mu} I_2 \right) I_F =$$

$$\Delta_H = 5.71 \text{ mm}$$

③ Design of pile footing

i) Design of pile located at A₁

$$V_{GK} = 455 \text{ kN}$$

$$V_{QK} = 273 \text{ kN}$$

Assume length $L = 14 \text{ m}$

pile diameter $D = 0.6 \text{ m}$

$$\text{self weight of pile } (W_{GK}) = \pi \times \left(\frac{D}{4}\right)^2 \times h \times \gamma_c$$

$$= \pi \times \frac{0.6^2}{4} \times 14 \times 25$$

$$W_{GK} = 98.9 \text{ kN}$$

calculations of design loads based on combination 1 & 2

$$V_d = \begin{bmatrix} 1.35 (455 + 98.9) + 1.5 \times 273 \\ 1 (455 + 98.9) + 1.3 \times 273 \end{bmatrix}$$

$$= \begin{bmatrix} 1157.265 \\ 908.8 \end{bmatrix} \text{ kN}$$

$$\text{pile shaft area } (A_s) = \pi \times D \times L$$

$$= \pi \times 0.6 \times 14$$

$$= 26.38 \text{ m}^2$$

pile base area

$$A_b = \frac{\pi \times D^2}{4} = \frac{\pi \times 0.6^2}{4}$$

$$= 0.282 \text{ m}^2$$

Bearing capacity factor $N_c = 9$

soil strata

layer depth (m)

layer 1

3m

layer 2

6m

layer 3

8m

layer 4

12m

layer 5

14m

* Average SPT value for layer 1 = $\left(\frac{23+26}{2}\right) = 24.5$

* Average SPT value for layer 2 = $\left(\frac{20+20+54}{3}\right) = 31.33$

* Average SPT value for layer 3 = $\frac{50}{1} = 50$

* Average SPT value for layer 4 = $\frac{43+49}{2} = 51$

* Average SPT value for layer 5 = $\frac{64}{1} = 64$

* undrained shear strength $C_u = SPT \times 5$

$$C_{u1} = 24.5 \times 5 = 122.5 \text{ kN/m}^2$$

$$C_{u2} = 31.33 \times 5 = 156.65 \text{ kN/m}^2$$

$$C_{u3} = 50 \times 5 = 250 \text{ kN/m}^2$$

$$C_{u4} = 51 \times 5 = 255 \text{ kN/m}^2$$

$$\therefore C_{u5} = 64 \times 5 = 320 \text{ kN/m}^2$$

From the graph adhesion factor at layer 5

$$f_{ss} = c_u \times 0.45 \times \left(\frac{\sigma_v}{c_u} \right)^{0.45}$$
$$= 320 \times 0.45 \times \left(\frac{87.32}{320} \right)^{0.45}$$

$$\therefore f_{ss} = 50.27 \text{ kN/m}^2$$

* pile shaft area $A_s = \pi \times D \times L$

$$= \pi \times 0.6 \times 14$$

$$= 26.38 \text{ m}^2$$

* Maximum shaft resistance (Q_s) = $A_s \times f_{ss}$

$$= 26.38 \times 50.27$$

$$= 2117.52 \text{ kN}$$

* pile base area = $\frac{\pi \times D^2}{4} = \frac{\pi \times 0.6^2}{4}$

$$= 0.2827 \text{ m}^2$$

* Unit base resistance $\frac{q}{b} = N \times c_u$

$$= 9 \times 320$$

$$= 2880 \text{ kN/m}^2$$

* Maximum base resistance $Q_b = \frac{\pi D^2}{4} \times \frac{q}{b}$

$$= \frac{\pi \times 0.6^2}{4} \times 2880$$

$$Q_b = 816.56 \text{ kN}$$

For bored pile the design resistance V_{RD} :-

ultimate bearing resistance ~~combination~~

$$V_{RD} = \left[\frac{Q_b}{1.25} + \frac{Q_s}{1} \right]$$
$$\left[\frac{Q_b}{1.6} + \frac{Q_s}{1.3} \right]$$

$$= \begin{bmatrix} \frac{816.58}{1.25} + \frac{2117.52}{1} \\ \frac{816.58}{1.6} + \frac{2117.52}{1.3} \end{bmatrix}$$

$$= \begin{bmatrix} 2770.76 \\ 2139.2 \end{bmatrix} \text{ kN}$$

$$\Delta GE_0 = \begin{bmatrix} 1157.26/2770.76 \\ 908.8/2139.2 \end{bmatrix} \times 100\% = \begin{bmatrix} 41.77\% \\ 42.48\% \end{bmatrix}$$

Ultimate total resistance ~~of combination~~ of

$$VRD_2 = \begin{bmatrix} \frac{Q_b + Q_s}{1.15} \\ \frac{Q_b + Q_s}{1.5} \end{bmatrix} = \begin{bmatrix} \frac{816.58 + 2117.52}{1.15} \\ \frac{816.58 + 2117.52}{1.5} \end{bmatrix}$$

$$= \begin{bmatrix} 2551.37 \\ 1956.05 \end{bmatrix} \text{ kN}$$

$$\therefore \Delta GE_0 = \frac{V_d}{VRD_2} \times 100\%$$

$$\Delta GE_0 = \begin{bmatrix} 1157.26/2551.37 \\ 908.8/1956.05 \end{bmatrix} \times 100\%$$

$$= \begin{bmatrix} 45.35\% \\ 46.46\% \end{bmatrix}$$

Settlement calculation:

$$Q_s = 2117.52 \text{ kN}$$

$$Q_b = 816.58 \text{ kN}$$

$$A_b = 0.2827 \text{ m}^2$$

$$A_s = 26.38 \text{ m}^2$$

$$E_p = 33 \times 10^6 \text{ kN/m}^2$$

$$E_b = 122500 \text{ kN/m}^2$$

Poisson's ratio $\mu = 0.35$

Influence factor of L/B ratio $I_p = 0.55$

* Pile head settlement based on combination 1

$$w_{s1} = \frac{Q_s}{1} = \frac{2117.52}{1} = 2117.52 \text{ kN}$$

$$w_{b1} = \frac{Q_b}{1} = \frac{816.57}{0.25} = 3266.28 \text{ kN}$$

$$\begin{aligned} \text{Pile head settlement } (P_1) &= \frac{(w_s + 2w_b)L}{2A_s E_p} + \left(\frac{\pi w_{b1}}{u A_b} \right) \times \left(\frac{D(1-\nu^2)I_p}{E_b} \right) \\ &= \left(\frac{(2117.52 + 2 \times 3266.28) \times 14}{2 \times 26.38 \times 33 \times 10^6} \right) + \left(\frac{\pi \times 3266.28}{u \times 0.2622} \right) \\ &\quad \times \left(\frac{0.6(1-0.35^2) \times 0.55}{1225000} \right) \\ &= 4.3 \times 10^{-3} \text{ m} \end{aligned}$$

$$P_1 = 4.3 \text{ mm}$$

* Pile head settlement based on head combination 2

$$w_{s2} = \frac{Q_s}{1.3} = \frac{2117.52}{1.3} = 1628.86 \text{ kN}$$

$$w_{b2} = \frac{Q_b}{1.6} = \frac{816.57}{1.6} = 510.35 \text{ kN}$$

Pile head settlement $P_2 =$

$$\begin{aligned} &= \frac{(w_{s2} + 2w_{b2})L}{2A_s E_p} + \left(\frac{\pi w_{b2}}{u A_b} \right) \times \left(\frac{D(1-\nu^2)I_p}{E_b} \right) \\ &= \left(\frac{(1628.86 + 2 \times 510.35) \times 14}{2 \times 26.38 \times 33 \times 10^6} \right) + \left(\frac{\pi \times 510.35}{u \times 0.2622} \right) \times \left(\frac{0.6(1-0.35^2) \times 0.55}{1225000} \right) \\ &= 2.13 \times 10^{-5} + 1417.85 \times 2.36 \times 10^{-6} \end{aligned}$$

$$P_2 = 3.3 \times 10^{-3} \text{ m} = 3.3 \text{ mm}$$

Both settlements P_1 & P_2 are less than 50mm

∴ This pile design is safe and acceptable

PILE HEAD RESISTANCE

ii

ii) Design of pile located at n_2 :-

Given data

$$V_{GK} = 314 \text{ kN}$$

$$V_{QK} = 73 \text{ kN}$$

Assume length $L = 11 \text{ m}$

pile diameter $D = 0.75 \text{ m}$

$$\begin{aligned} \text{weight of pile (} w_{pile} \text{)} &= \pi \times \frac{D^2}{4} \times L \times \gamma_c \\ &= \pi \times \frac{0.75^2}{4} \times 11 \times 25 \\ &= 154.59 \end{aligned}$$

∴ calculating design loads based on combination

$$V_d = \begin{bmatrix} 1.35(314 + 154.59) + 1.5 \times 73 \\ 1(314 + 154.59) + 1.3 \times 73 \end{bmatrix}$$

$$= \begin{bmatrix} 742.1 \\ 563.49 \end{bmatrix} \text{ kN}$$

Bearing capacity factor $N_c = 9$

— Average SPT layer 1 at $(\frac{23+26}{2}) = 24.5$

SPT layer 2 $(\frac{20+20.04}{3}) = 31.33$

SPT layer 3 $(\frac{50}{1}) = 50$

SPT layer 4 $(\frac{43+54}{2}) = 51$

SPT layer 5 $(\frac{64}{1}) = 64$

∴ undrained shear strength $C_u = \text{SPT} \times 5$

$$C_{u1} = 14.5 \times 5 = 122.5 \text{ kN/m}^2$$

$$C_{u2} = 21.33 \times 5 = 156.65 \text{ kN/m}^2$$

$$C_{u3} = 50 \times 5 = 250 \text{ kN/m}^2$$

$$C_{u4} = 57 \times 5 = 265 \text{ kN/m}^2$$

$$\boxed{C_{u5} = 64 \times 5 = 320 \text{ kN/m}^2}$$

From the graph adhesion factor at layer 5

$$\begin{aligned} f_{cs} &= \bar{C}_u \times 0.45 \times \left(\frac{\bar{C}_u}{\bar{C}_1} \right)^{0.45} \\ &= 320 \times 0.45 \times \left(\frac{320}{265} \right)^{0.45} \\ &= 80.27 \text{ kN/m}^2 \end{aligned}$$

pile shaft area $A_s = \pi \times D \times L$

$$\begin{aligned} &= \pi \times 0.75 \times 14 \\ &= 32.98 \text{ m}^2 \end{aligned}$$

Maximum shaft resistance

$$\begin{aligned} Q_s &= A_s \times f_{cs} \\ &= 32.98 \times 80.27 \end{aligned}$$

$$Q_s = 2647.30 \text{ kN}$$

pile for bored pile design resistance :

ultimate bearing resistance

$$V_{Rd1} = \left[\begin{array}{c} \frac{Q_b}{1.25} + \frac{Q_s}{1} \\ \frac{Q_b}{1.6} + \frac{Q_s}{1.3} \end{array} \right]$$

$$\text{pile base area} = \frac{\pi \times D^2}{4} = \frac{\pi \times 0.71^2}{4}$$

$$= 0.4419 \text{ m}^2$$

$$\text{unit base resistance } \frac{q}{b} = N \times C_{up}$$

$$= 9 \times 320$$

$$= 2880 \text{ kN/m}^2$$

$$\text{Maximum base resistance } Q_b = \frac{\pi D^2}{4} \times \frac{q}{b}$$

$$Q_b = 1272 \text{ kN}$$

∴ ultimate bearing resistance

$$VRD1 = \left[\frac{1272}{1.25} + \frac{2647.30}{1} \right]$$

$$\left[\frac{1272}{1.6} + \frac{2647.30}{1.3} \right]$$

$$= \left[\begin{array}{c} 3664.9 \\ 2831.38 \end{array} \right] \text{ kN}$$

$$\therefore \Delta G E_0 = \left[\begin{array}{c} 742.1 / 3664.9 \\ 563.49 / 2831.38 \end{array} \right] \times 100 = \left[\begin{array}{c} 20.25\% \\ 19.9\% \end{array} \right]$$

ultimate total resistance

$$= \left[\begin{array}{c} \frac{Q_b + Q_s}{1.15} \\ \frac{Q_b + Q_s}{1.5} \end{array} \right] = \left[\begin{array}{c} \frac{1272 + 2647.30}{1.15} \\ \frac{1272 + 2647.30}{1.5} \end{array} \right]$$

$$= \left[\begin{array}{c} 3574 \\ 3036.58 \end{array} \right] \text{ kN}$$

$$\therefore \Delta G E_0 = \begin{bmatrix} 742.1 / 3554.0 \\ 573.49 / 3036.86 \end{bmatrix} \times 100 = \begin{bmatrix} 20.76\% \\ 18.56\% \end{bmatrix} \textcircled{4}$$

settlement check:
Obtained values

$$Q_s = 2647.30 \text{ kN}$$

$$Q_b = 1272 \text{ kN}$$

$$A_b = 0.4417 \text{ m}^2$$

$$A_s = 32.98 \text{ m}^2$$

$$E_p = 33 \times 10^6 \text{ kN/m}^2$$

$$E_b = 132500 \text{ kN/m}^2$$

$$\text{poisson's ratio } \nu = 0.35$$

Influence factor of $\frac{L}{B}$ ratio $I_p = 0.75$

\therefore pile head settlement based on combination 1

$$W_{S1} = \frac{Q_s}{1} = \frac{2647.30}{1} = 2647.30 \text{ kN}$$

$$W_{B1} = \frac{Q_b}{1.25} = \frac{1272}{1.25} = 1017.6 \text{ kN}$$

$$\begin{aligned} \text{pile head settlement } (P_1) &= \frac{(W_{S1} + 2W_{B1})}{2A_s \times E_p} + \frac{W_{B1}}{4A_b} \left(\frac{p(1-\nu^2)I_p}{E_b} \right) \\ &= \frac{(2647.30 + 2 \times 1017.6) \times 14}{2 \times 32.98 \times 33 \times 10^6} + \left(\frac{1 \times 1017.6}{4 \times 0.4417} \right) \times \left(\frac{0.75(1-0.35^2) \times 0.75}{132500} \right) \end{aligned}$$

$$P_1 = 5.31 \text{ mm}$$

pile head settlement based on load combination 2

$$W_{S2} = \frac{Q_s}{1.3} = \frac{2647.30}{1.3} = 2036.76 \text{ kN}$$

$$wb_2 = \frac{Q_b}{1.6} = \frac{1017.6}{1.6} = 636 \text{ kN}$$

$$P_2 = \frac{(ws_2 + 2wb_2) \times L}{2 \times E_p} + \frac{\pi wb_2}{4 A_b} \times \left(\frac{D(1-\nu^2) I_p}{E_b} \right)$$

$$= \left[\frac{(2036.38 + 2 \times 636) \times 14}{2 \times 32.98 \times 333 \times 10^6} \right] + \left(\frac{\pi \times 636}{4 \times 0.4417} \right) \times \left(\frac{0.75 \times (1 - 0.35^2) \times 0.55}{12250} \right)$$

$$P_2 = 8.3 \times 10^{-3} \text{ m}$$

Both settlement P_1 & P_2 are less than 50mm

\therefore The pile design is safe and acceptable.

ii) Design of located at B₁

$$\text{Vertical load } V_{Gk} = \overset{836}{\cancel{301}} \text{ kN}$$

$$\text{Vertical load } V_{Qk} = 198 \text{ kN}$$

Assume length $L = 14 \text{ m}$

$$\text{pile diameter } D = 0.9 \text{ m}$$

$$\begin{aligned} \text{weight of pile } (w_{Gk}) &= \pi \times \frac{D^2}{4} \times h \times \rho_c \\ &= \pi \times \frac{0.9^2}{4} \times 14 \times 25 \end{aligned}$$

$$w_{Gk} = 222.66$$

∴ calculating design loads based on combination 1.3.2

$$\begin{aligned} V_d &= \begin{bmatrix} 1.35(836 + 222.66) + 1.5(198) \\ 1(836 + 222.66) + 1.3(198) \end{bmatrix} \\ &= \begin{bmatrix} 1726.9 \\ 1316.06 \end{bmatrix} \text{ kN} \end{aligned}$$

Bearing capacity factor $N_c = 9$

$$\text{Avg SPT layer 1 } \left(\frac{25 + 26}{2} \right) = 24.5$$

$$\text{SPT layer 2 } \left(\frac{20 + 20 + 31}{3} \right) = 31.33$$

$$\text{SPT layer 3 } \left(\frac{50}{1} \right) = 50$$

$$\text{SPT layer 4 } \left(\frac{43 + 51}{2} \right) = 57$$

$$\text{SPT layer 5 } \left(\frac{64}{1} \right) = 64$$

∴ undrained shear strength

$$q_u = sPT \times 5$$

$$C_{u1} = 14.5 \times 5 = 122.5 \text{ kN/m}^2$$

$$C_{u2} = 31.33 \times 5 = 156.65 \text{ kN/m}^2$$

$$C_{u3} = 50 \times 5 = 250 \text{ kN/m}^2$$

$$C_{u4} = 51 \times 5 = 265 \text{ kN/m}^2$$

$$C_{u5} = 64 \times 5 = 320 \text{ kN/m}^2$$

From the graph adhesion factor at layer 5

$$f_{cs} = \bar{C}_u \times 0.45 \times \left(\frac{\bar{\sigma}_v}{\bar{C}_u} \right)^{0.45}$$

$$f_{cs} = 320 \times 0.45 \times \left(\frac{87.33}{320} \right)^{0.45}$$

$$f_{cs} = 80.27 \text{ kN/m}^2$$

$$\begin{aligned} \therefore \text{pile shaft area } A_s &= \pi \times D \times L \\ &= \pi \times 0.9 \times 14 \\ &= 39.58 \text{ m}^2 \end{aligned}$$

∴ Maximum shaft resistance

$$\begin{aligned} Q_s &= A_s \times f_{cs} \\ &= 39.58 \times 80.27 \\ &= 3177.08 \text{ kN} \end{aligned}$$

$$\text{pile base area} = \frac{\pi \times D^2}{4} = \frac{\pi \times 0.9^2}{4} = 0.636 \text{ m}^2$$

$$\begin{aligned} \text{unit base resistance } q/b &= N \times C_{u5} \\ &= 9 \times 320 \\ &= 2880 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \therefore \text{Maximum base resistance } Q_b &= \frac{\pi D^2}{4} \times q/b \\ &= 0.636 \times 2880 \\ Q_b &= 1831.68 \text{ kN} \end{aligned}$$

For bored pile design resistance :

ultimate bearing resistance

$$V_{RD1} = \begin{bmatrix} \frac{Q_b}{1.25} + \frac{Q_s}{1} \\ \frac{Q_b}{1.6} + \frac{Q_s}{1.3} \end{bmatrix} = \begin{bmatrix} \frac{1831.6}{1.25} + \frac{3177.08}{1} \\ \frac{1831.6}{1.6} + \frac{3177.08}{1.3} \end{bmatrix}$$

$$= \begin{bmatrix} 4642.52 \\ 4321.75 \end{bmatrix}$$

$$\therefore A G E_0 = \begin{bmatrix} 1726.19 / 4642.52 \\ 1316.06 / 4321.75 \end{bmatrix} \times 100 = \begin{bmatrix} 37.18\% \\ 30.45\% \end{bmatrix}$$

ultimate total resistance at combination 1 & 2

$$V_{RD2} = \begin{bmatrix} \frac{Q_b + Q_s}{1.15} \\ \frac{Q_b + Q_s}{1.5} \end{bmatrix} = \begin{bmatrix} \frac{1831.68 + 3177.08}{1.15} \\ \frac{1831.68 + 3177.08}{1.5} \end{bmatrix}$$

$$= \begin{bmatrix} 4594.35 \\ 3949.72 \end{bmatrix} \text{ kN}$$

$$\therefore A G E_0 = \begin{bmatrix} 1726.19 / 4594.35 \\ 1316.06 / 3949 \end{bmatrix} \times 100 = \begin{bmatrix} 37.58\% \\ 33.32\% \end{bmatrix}$$

∴ settlement calculation :

obtained values : $Q_s = 3177.08 \text{ kN}$

$Q_b = 1831.68 \text{ kN}$

$$A_b = 0.636 \text{ m}^2$$

$$A_s = 39.58 \text{ m}^2$$

$$E_p = 33 \times 10^6 \text{ kN/m}^2$$

$$E_b = 12250 \text{ kN/m}^2$$

Poisson's ratio $\nu = 0.35$

Influence factor of L/b ratio $I_p = 0.55$

pile head settlement based on combination 1

$$w_{s1} = \frac{Q_s}{1} = \frac{3177.08}{1} = 3177.08 \text{ kN}$$

$$w_{b1} = \frac{Q_b}{1.25} = \frac{1831.68}{1.25} = 1465.34 \text{ kN}$$

pile head settlement (P_1) =
$$\frac{(w_{s1} + 2w_{b1}) \times L}{2 \times A_s \times E_p} + \frac{\pi w_{b1}}{4 A_b} \times \left(\frac{D(1-\nu^2) I_p}{E_b} \right)$$

$$= \left(\frac{(3177.08 + 2 \times 1465.34) \times 14}{2 \times 39.58 \times 33 \times 10^6} \right) + \left(\frac{\pi \times 1465.34}{4 \times 0.636} \right) \times \left(\frac{0.9(1-0.35^2) \times 0.55}{12250} \right)$$

$$= 6.4 \times 10^{-3} \text{ m}$$

$$P_1 = 6.4 \text{ mm}$$

pile head settlement based on load combination 1 & 2

$$w_{s2} = \frac{Q_s}{1.3} = \frac{3177.08}{1.3} = 2443.9 \text{ kN}$$

$$w_{b2} = \frac{Q_b}{1.6} = \frac{1831.68}{1.6} = 1144.8 \text{ kN}$$

$$P_2 = \left(\frac{(w_{s2} + 2w_{b2}) \times L}{2 A_s E_p} \right) + \left(\frac{\pi w_{b2}}{4 A_b} \right) \times \left(\frac{D(1-\nu^2) I_p}{E_b} \right)$$

$$= \left[\frac{(2443.9 + 2 \times 1144.8) \times 14}{2 \times 39.58 \times 33 \times 10^6} \right] + \left[\frac{\pi \times 1144.8}{4 \times 0.636} \right] \times \left[\frac{0.9(1-0.35^2) \times 0.55}{12250} \right]$$

$$P_2 = 5 \times 10^{-3} \text{ m} = 5 \text{ mm}$$

both settlements P_1 & P_2 are less than 50mm

∴ The pile design is safe and acceptable.

①
iv) Design of pile located at B₂:-

$$\text{Vertical load } V_{GE} = 319 \text{ kN}$$

$$\text{Vertical load } V_{AB} = 99 \text{ kN}$$

Assume length $L = 14 \text{ m}$

$$\text{pile diameter } D = 1.05 \text{ m}$$

$$\begin{aligned} \text{weight of pile } (w_{pile}) &= \pi \times \frac{D^2}{4} \times L \times \rho_c \\ &= \pi \times \frac{1.05^2}{4} \times 14 \times 25 \\ &= 302.37 \text{ kN} \end{aligned}$$

* calculating design loads based on combination 1 & 2

$$\begin{aligned} V_d &= \left[\begin{array}{l} 1.35(319 + 302.37) + 1.5 \times 99 \\ 1(319 + 302.37) + 1.3 \times 99 \end{array} \right] \\ &= \left[\begin{array}{l} 987.38 \\ 750.07 \end{array} \right] \text{ kN} \end{aligned}$$

Bearing capacity factor $N_c = 9$

$$\text{Avg SPT layer 1 } \left(\frac{23+26}{2} \right) = 24.5$$

$$\text{SPT layer 2 } \left(\frac{20+20+54}{3} \right) = 31.33$$

$$\text{SPT layer 3 } \left(\frac{50}{1} \right) = 50$$

$$\text{SPT layer 4 } \left(\frac{42+41}{3} \right) = 31.33$$

$$\text{SPT layer 5 } \left(\frac{64}{1} \right) = 64$$

∴ undrained shear strength

$$C_u = \text{SPT} \times 5$$

$$C_{u1} = 14.5 \times 5 = 122.5 \text{ kN/m}^2$$

$$C_{u2} = 31.33 \times 5 = 156.5 \text{ kN/m}^2$$

$$C_{u3} = 50 \times 5 = 250 \text{ kN/m}^2$$

$$C_{u4} = 57 \times 5 = 285 \text{ kN/m}^2$$

$$C_{u5} = 64 \times 5 = 320 \text{ kN/m}^2$$

From the graph adhesion factor at layer 5

$$f_{as} = \bar{C}_u \times 0.45 \times \left(\frac{\bar{\sigma}_v}{\bar{C}_u} \right)^{0.45}$$

$$f_{as} = 320 \times 0.45 \times \left(\frac{87.33}{320} \right)^{0.45}$$
$$= 80.27 \text{ kN/m}^2$$

pile shaft area $A_s = \pi \times D \times L$

$$= \pi \times 1.05 \times 14$$

$$= 46.18 \text{ m}^2$$

Maximum shaft resistance

$$Q_s = A_s \times f_{as}$$

$$= 46.18 \times 80.27$$

$$= 3706.9 \text{ kN}$$

$$\text{pile base area} = \frac{\pi \times D^2}{4} = 0.865 \text{ m}^2$$

$$\text{unit base resistance } q/b = N \times C_{u5}$$

$$= 9 \times 320$$

$$q/b = 2880 \text{ kN/m}^2$$

$$\text{maximum base resistance } Q_b = \frac{\pi D^2}{4} \times q/b$$

$$= 0.865 \times 2880$$

$$Q_b = 2491.2 \text{ kN}$$

For bored pile resistance V_{Rd}

ultimate bearing resistance combination 1 & 2

$$V_{Rd(1)} = \begin{bmatrix} \frac{Q_b}{1.25} + \frac{Q_s}{1} \\ \frac{Q_b}{1.6} + \frac{Q_s}{1.3} \end{bmatrix} = \begin{bmatrix} \frac{2491.2}{1.25} + \frac{3706.9}{1} \\ \frac{2491.2}{1.6} + \frac{3706.9}{1.3} \end{bmatrix}$$

$$= \begin{bmatrix} 5699.86 \\ 4408.46 \end{bmatrix} \text{ kN}$$

$$\Delta GE_0 = \begin{bmatrix} 987.35/5699.86 \\ 750.07/4408.46 \end{bmatrix} \times 100 = \begin{bmatrix} 17.32\% \\ 17.01\% \end{bmatrix}$$

ultimate total resistance at combination 1 & 2

$$V_{Rd(2)} = \begin{bmatrix} \frac{Q_b + Q_s}{1.15} \\ \frac{Q_b + Q_s}{1.5} \end{bmatrix} = \begin{bmatrix} \frac{2491.2 + 3706.9}{1.15} \\ \frac{2491.2 + 3706.9}{1.5} \end{bmatrix}$$

$$= \begin{bmatrix} 5389.6 \\ 4132.06 \end{bmatrix} \text{ kN}$$

$$\therefore \Delta GE_0 = \begin{bmatrix} 987.35/5389.6 \\ 750.07/4132.06 \end{bmatrix} \times 100 = \begin{bmatrix} 18.32\% \\ 18.15\% \end{bmatrix}$$

Settlement calculation

we have

$Q_s = 3706.9 \text{ kN}$

$Q_b = 2491.2 \text{ kN}$

$A_b = 0.865 \text{ m}^2$

$A_s = 46.18 \text{ m}^2$

$$E_p = 33 \times 10^6 \text{ kN/m}^2$$

$$E_b = 122500 \text{ kN/m}^2$$

Poisson's ratio $\nu = 0.35$

Influence factor of L/B ratio $I_p = 0.55$

pile head settlement based on combination 1

$$W_{S1} = \frac{Q_s}{1} = \frac{3706.9}{1} = 3706.9 \text{ kN}$$

$$W_{B1} = \frac{Q_b}{1.25} = \frac{2491.2}{1.25} = 1992.96 \text{ kN}$$

$$\text{pile head settlement } (P_1) = \frac{(W_{S1} + 2W_{B1}) \times L}{2A_s \times E_p} + \left(\frac{\pi W_{B1}}{4A_b} \right) \times \left(\frac{D(1-\nu^2)I_p}{E_b} \right)$$

$$= \left(\frac{3706.9 + 2 \times 1992.96 \times 14}{2 \times 46.18 \times 33 \times 10^6} \right) + \left(\frac{\pi \times 1992.96}{4 \times 0.865} \right) \times \left(\frac{1.05(1-0.35^2)0.55}{122500} \right)$$

$$= 75 \times 10^{-3} \text{ m}$$

$$= 7.5 \text{ mm}$$

pile head settlement based on load combination 2

$$W_{S2} = \frac{Q_s}{1.3} = \frac{3706.9}{1.3} = 2851.46 \text{ kN}$$

$$W_{B2} = \frac{Q_b}{1.6} = \frac{2491.2}{1.6} = 1557 \text{ kN}$$

$$P_2 = \left(\frac{(W_{S2} + 2W_{B2}) \times L}{2A_s \times E_p} \right) + \left(\frac{\pi W_{B2}}{4A_b} \right) \times \left(\frac{D(1-\nu^2)I_p}{E_b} \right)$$

$$= \left(\frac{(2851.46 + 2 \times 1557) \times 14}{2 \times 46.18 \times 33 \times 10^6} \right) + \left(\frac{\pi \times 1557}{4 \times 0.865} \right) \times \left(\frac{1.05(1-0.35^2)0.55}{122500} \right)$$

$$= 5.8 \times 10^{-3} \text{ m}$$

$$P_2 = 5.8 \text{ mm}$$

Both settlement P_1 & P_2 are less than 50 mm

∴ The pile design is safe and acceptable.