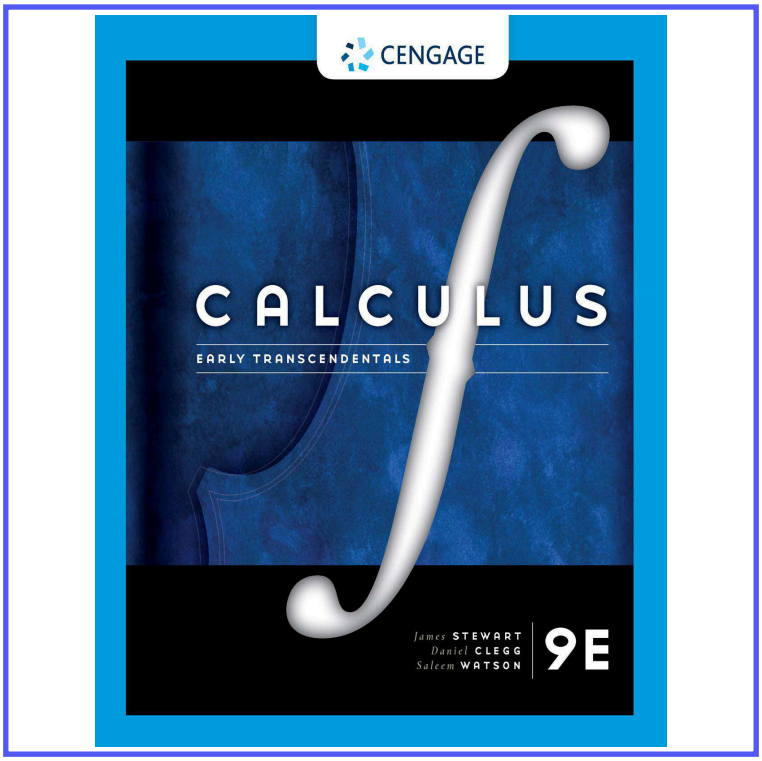


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***Calculus: Early Transcendentals,* Ninth Edition**
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Library of Congress Control Number: 2019948283

Student Edition:
ISBN: 978-1-337-61392-7

Loose-leaf Edition:
ISBN: 978-0-357-02229-0

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Printed in the United States of America
Print Number: 01 Print Year: 2019

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