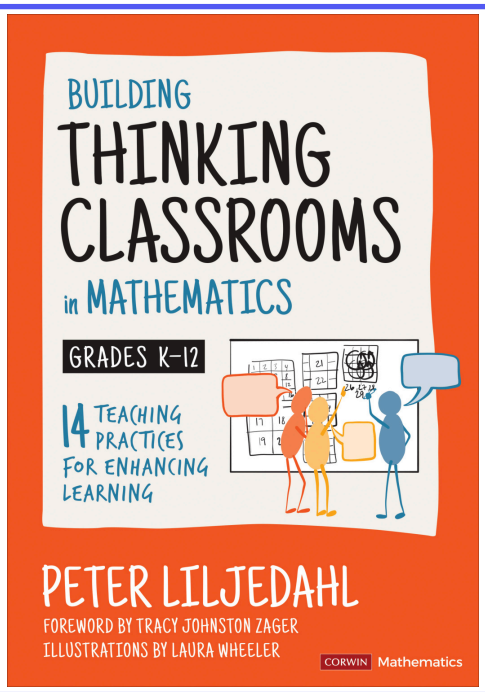



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# BUILDING THINKING CLASSROOMS IN MATHEMATICS

GRADES K-12

For every teacher who has had the courage to change.

# BUILDING THINKING CLASSROOMS IN MATHEMATICS

## 14 Teaching Practices for Enhancing Learning

## GRADES K–12

**Peter Liljedahl**

**Foreword by Tracy Johnston Zager**
**Illustrations by Laura Wheeler**

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*For information:*

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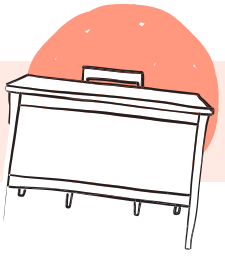
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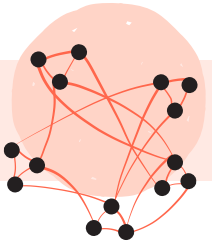
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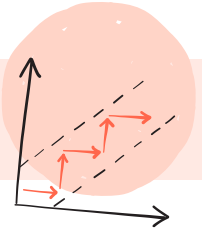
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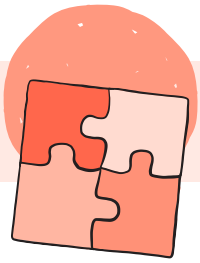
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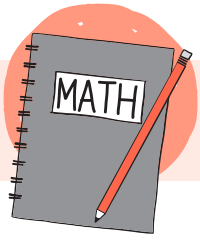
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